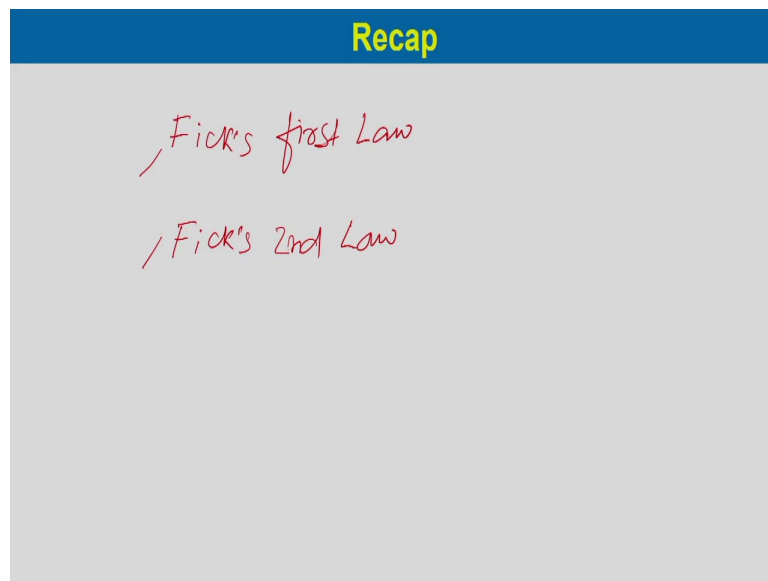


Mass Transfer Operations - I
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Diffusion Mass Transfer
Lecture – 04
Steady State Molecular Diffusion in fluids under stagnant and laminar flow conditions

Welcome to the 4th lecture on Mass Transfer Operations. In this lecture, we will discuss the diffusion mass transfer in particular to the Steady State Molecular Diffusion under stagnant and laminar flow conditions. Before going to the lecture let us have small recap on the previous lecture. In the previous lecture we have considered the Fick's law of diffusions and we have considered study state diffusion and unsteady state diffusion.

(Refer Slide Time: 01:11)



In study sate diffusion we discuss the Fick's first law and the second case we have discussed the Fick's second law which is applicable for unsteady state diffusion.

(Refer Slide Time: 01:47)

Steady State Molecular Diffusion in Fluids Under Stagnant and Laminar Flow Conditions

Steady state diffusion through a constant area :

- Assume steady state diffusion in the x-direction without any chemical reaction in a binary gaseous mixture of species A and B.
- For one dimensional diffusion of species A, molar flux:
$$N_A = -CD_{AB} \frac{dy_A}{dx} + y_A N$$

Where $N = N_A + N_B$
- Separating the variables in equation (a), it can be expressed as:
$$\frac{-dy_A}{N_A - y_A N} = \frac{dx}{CD_{AB}}$$

Now, steady state molecular diffusion in fluids under stagnant and laminar flow conditions. Steady state diffusion through a constant area if we consider and then we assume that steady state diffusion in the x direction without any chemical reactions in a binary gaseous mixture of species A and B for one dimensional diffusions of species A.

We know the molar flux equations N_A is equal to minus $CD_{AB} \frac{dy_A}{dx}$ plus $y_A N$ this is N is the total mole molar flux is equal to N_A plus N_B . Now, separating the variables in this equations this equation can be expressed as minus dy_A divided by $N_A - y_A N$ is equal to dx by CD_{AB} so this is equation b.

(Refer Slide Time: 03:01)

Steady State Molecular Diffusion Through a Constant Area

- For the gaseous mixture, at constant pressure and temperature, C and D_{AB} are constant, independent of position and composition. Also all the molar fluxes are constant in equation (b). Therefore the equation (b) can be integrated between two boundary conditions as follows:

$$\frac{-dy_A}{N_A - y_A N} = \frac{dx}{CD_{AB}}$$

b

•at $x = x_1, \quad y_A = y_{A1}$

•at $x = x_2, \quad y_A = y_{A2}$ ✓

Where,

1, indicates the start of the diffusion path.

2, indicates the end of the diffusion path.

Now, for the gaseous mixture at constant pressure and temperature the concentration and diffusion coefficient D_{AB} are constant and independent of position and composition also all the molar fluxes are constant in equation b, equation b is minus dy_A divided by $N_A - y_A N$ is equal to dx / CD_{AB} .

Therefore, the equation b can be integrated between the 2 boundary conditions which is given as follows at x is equal to x_1 y_A would be equal to y_{A1} , y_A is the mole fractions of component A in the gas phase. At x is equal to x_2 y_A would be equal to y_{A2} , y_{A2} is the mole fractions of component 2 in the gas phase. So, 1 indicates the start of diffusion path and 2 indicates the end of the diffusion path.

(Refer Slide Time: 04:15)

Steady State Molecular Diffusion Through a Constant Area

Integrating eq (b) with the above BC's:

$$\int_{y_{A1}}^{y_{A2}} \frac{-dy_A}{N_A - y_A N} = \int_{x_1}^{x_2} \frac{dx}{CD_{AB}}$$

Let,

$$N_A - y_A N = Z$$

$$\Rightarrow -dy_A N = dZ$$

$$\Rightarrow -dy_A = \frac{dZ}{N}$$

Substituting the values in above equation,

$$\int_{Z_1}^{Z_2} \frac{dZ}{NZ} = \int_{x_1}^{x_2} \frac{dx}{CD_{AB}}$$

Now, if we integrate equation b with the above boundary conditions we can get integral y_{A1} to y_{A2} minus dy_A divided by $N_A - y_A N$ is equal to integral x_1 to x_2 dx by CD_{AB} . Let $N_A - y_A N$ would be equal to Z . So, from here we can write minus $dy_A N$ would be equal to dZ and minus dy_A would be equal to dZ by N .

So, substituting the values in the above equations minus dy_A it would be integral Z_1 to Z_2 dZ by NZ would be equal to integral x_1 to x_2 dx by CD_{AB} . So, since $N_A - y_A N$ is Z . So, it is Z and minus dy_A over here which is substituted by dZ by N . So, it becomes integral Z_1 to Z_2 dZ by N into Z is equal to integral x_1 to x_2 dx by CD_{AB} .

(Refer Slide Time: 06:01)

Steady State Molecular Diffusion Through a Constant Area

$$\int_{Z_1}^{Z_2} \frac{dZ}{NZ} = \int_{x_1}^{x_2} \frac{dx}{CD_{AB}} \quad \text{Or,} \quad \frac{1}{N} (\ln Z_2 - \ln Z_1) = \frac{1}{CD_{AB}} (x_2 - x_1)$$

$$\Rightarrow \ln \left(\frac{Z_2}{Z_1} \right) = \frac{N}{CD_{AB}} (x_2 - x_1) \quad \checkmark$$

$$\Rightarrow \ln \left(\frac{N_A - y_{A_2} N}{N_A - y_{A_1} N} \right) = \frac{N}{CD_{AB}} (x_2 - x_1) \quad \checkmark$$

$$\Rightarrow \ln \left[\frac{N \left(\frac{N_A}{N} - y_{A_2} \right)}{N \left(\frac{N_A}{N} - y_{A_1} \right)} \right] = \frac{N}{CD_{AB}} (x_2 - x_1) \quad \checkmark$$

➤ Multiplying both sides with N_A in above equation,

Now, integral Z_1 to Z_2 dZ by NZ equal to integral x_1 to x_2 dx CD_{AB} can be written as $\frac{1}{N} \ln Z_2 - \ln Z_1$ is equal to $\frac{1}{CD_{AB}} (x_2 - x_1)$ and from that if we rearrange it would be $\ln \frac{Z_2}{Z_1}$ is equal to $\frac{N}{CD_{AB}} (x_2 - x_1)$. Now, if we substitute Z at Z_1 and Z_2 then it would be $\ln \frac{N_A - y_{A_2} N}{N_A - y_{A_1} N}$ would be equal to $\frac{N}{CD_{AB}} (x_2 - x_1)$.

So, it would be $\ln \frac{N \left(\frac{N_A}{N} - y_{A_2} \right)}{N \left(\frac{N_A}{N} - y_{A_1} \right)}$. If we just multiply both numerator and the denominator by N it would be like this the left hand side equation and the right hand side equations should be $\frac{N}{CD_{AB}} (x_2 - x_1)$. Now, if we multiply both sides with N_A in this equation.

(Refer Slide Time: 07:51)

Steady State Molecular Diffusion Through a Constant Area

$$\Rightarrow N_A = \frac{N_A}{N} \times \frac{CD_{AB}}{(x_2 - x_1)} \ln \left[\frac{\left(\frac{N_A}{N} - y_{A2}\right)}{\left(\frac{N_A}{N} - y_{A1}\right)} \right]$$

- Therefore, after integration with the boundary conditions the equation for diffusion for the said condition can be expressed as

$$N_A = \frac{N_A}{N} \frac{CD_{AB}}{x_2 - x_1} \ln \left[\frac{\frac{N_A}{N} - y_{A2}}{\frac{N_A}{N} - y_{A1}} \right] \quad \text{c}$$

We will obtain N_A would be equal to N_A by N into $C D_{AB}$ by x_2 minus x_1 \ln N_A by N minus y_{A2} divided by N_A by N minus y_{A1} . Therefore, after integration with the boundary conditions the equation for diffusion for the said conditions can be expressed as this relations. So, N_A would be equal to N_A by $N C D_{AB}$ by x_2 minus x_1 \ln N_A by N minus y_{A2} divided by N_A by N minus y_{A1} .

(Refer Slide Time: 08:41)

Steady State Diffusion through Non-Diffusing B:

- For steady state one dimensional diffusion of A through non-diffusing B, $N_B = 0$ and $N_A = \text{constant}$. Therefore,

$$\frac{N_A}{N} = \frac{N_A}{N_A + N_B} = 1$$

- Hence equation (c) becomes:

$$\text{d} \quad N_A = \frac{CD_{AB}}{x_2 - x_1} \ln \left[\frac{1 - y_{A2}}{1 - y_{A1}} \right]$$

For, an ideal gas, $C = \frac{P_t}{RT}$

For, mixture of ideal gases, $y_A = \frac{p_A}{P_t}$ ✓

- The equation (d) can be expressed in terms of partial pressures as:

$$\text{e} \quad N_A = \frac{D_{AB} P_t}{(x_2 - x_1) RT} \ln \left[\frac{P_t - p_{A2}}{P_t - p_{A1}} \right]$$

Where,

P_t = total pressure

p_{A1} and p_{A2} = partial pressures of A at point 1 and 2 respectively. ✓

Now, steady state diffusion through non diffusing B, for steady state one dimensional diffusion of A through non diffusing B N_B would be equal to 0 and N_A would be equal

to constant. Therefore, the N_A by N would be equal to N_A by N_A plus N_B would be equal to 0. Since N_B is equal to 0. So, N_A by N_A plus N_B would be equal to N_A by N_A would be equal to 1. Hence equation c becomes N_A is equal to $C D A B \times 2$ minus x_1 $\ln \frac{1 - y_{A2}}{1 - y_{A1}}$.

For an ideal gas we can write concentration would be equal to total pressure P_t divided by RT R is the universal gas constant and T is any temperature. For mixture of ideal gases the mole fractions y_A in the gas phase can be expressed as the partial pressure of that component divided by the total pressure. The equation d can be expressed in terms of the partial pressures as follows; N_A would be equal to $D A B P_t$ divided by x_2 minus $x_1 RT \ln \frac{P_t - P_{A2}}{P_t - P_{A1}}$. Where P_t is the total pressure P_{A1} and P_{A2} are the partial pressures of A at point 1 and 2 respectively.

(Refer Slide Time: 10:41)

Steady State Diffusion through Non-Diffusing B:

- For diffusion under turbulent conditions, the flux is usually calculated based on linear driving force. For this purpose the equation (e) can be manipulated to rewrite it in terms of a linear driving force.
- Since for the binary gas mixture of total pressure P_t , $P_t = p_A + p_B$

$$P_t - p_{A_2} = p_{B_2} \quad \& \quad P_t - p_{A_1} = p_{B_1} \quad \longrightarrow \quad p_{A_1} - p_{A_2} = p_{B_2} - p_{B_1}$$

- Then the equation (e) can be written as:

$$N_A = \frac{D_{AB} P_t}{RT(x_2 - x_1)} \left[\frac{p_{A_1} - p_{A_2}}{p_{B_2} - p_{B_1}} \right] \ln \left[\frac{p_{B_2}}{p_{B_1}} \right]$$

Or,

$$N_A = \frac{D_{AB} P_t}{RT(x_2 - x_1) p_{B,M}} (p_{A_1} - p_{A_2})$$

For diffusion under turbulent conditions the flux is usually calculated based on linear driving force for this purpose the equation e can be manipulated to rewrite in terms of a linear driving force. Since for binary gas mixture of total pressure P_t we can write P_t is equal to P_A plus P_B . P_A and P_B are the partial pressure of component A and component B. So, that we can write P_t minus P_{A2} would be equal to P_{B2} and P_t minus P_{A1} would be equal to P_{B1} .

Hence, we can write P_{A1} minus P_{A2} would be equal to P_{B2} minus P_{B1} . Then the equation e can be written as N_A would be equal to $D A B P_t$ divided by $RT \times 2$ minus x

1 in to P A 1 minus P A 2 divided by P B 2 minus P B 1 into ln P B 2 by P B 1. So, we can rearrange this relation as N A would be equal to D A B Pt by RT x 2 minus x 1 P B LM into P A 1 minus P A 2.

(Refer Slide Time: 12:21)

Steady State Diffusion through Non-Diffusing B:

$$N_A = \frac{D_{AB} P_t}{RT(x_2 - x_1) p_{B,LM}} (p_{A_1} - p_{A_2})$$

Where $p_{B,LM}$ = logarithmic mean partial pressure of species B which is defined as:

$$p_{B,LM} = \frac{p_{B_2} - p_{B_1}}{\ln\left(\frac{p_{B_2}}{p_{B_1}}\right)}$$

➤ The component A diffuses by concentration gradient: $-\frac{dy_A}{dx}$

- Here flux is inversely proportional to the distance through which diffusion occurs and the concentration of the stagnant gas ($p_{B,LM}$) because with increase in x and $p_{B,LM}$ resistance increases and flux decreases.

In this relation P B LM is the logarithmic mean of partial pressure of species B which is defined as P B LM is equal to P B 2 minus P B 1 divided by ln P B 2 by P B 1. The component A diffuses by concentration gradients the gradient is minus d y A d x. Here flux is inversely proportional to the distance through which the diffusion occurs and the concentration of the stagnant gas that is in terms of the logarithmic mean of partial pressures of species B. Because with increase in x and P B LM resistance increases and flux decreases.

(Refer Slide Time: 13:23)

Steady State Diffusion through Non-Diffusing B:

$$N_A = \frac{D_{AB} P_1}{RT(x_2 - x_1) P_{BLM}} (P_{A_1} - P_{A_2})$$

- Here flux is inversely proportional to the distance through which diffusion occurs and the concentration of the stagnant gas (P_{BLM}) because with increase in x and P_{BLM} resistance increases and flux decreases.

This change of concentration or the partial pressure can be expressed in terms of the simple profiles which is shown over here y axis p_A or p_B in terms of say atmosphere and x axis is the distance may be represented by z . So, which varies from 0 0.2 0.4 0.6 0.8 and 1.0 and this partial pressure can vary from.

So, this is the variation of concentration of p_{A2} to p_{A1} and the concentration variation of p_B can be expressed p_{B1} . So, P_t is the total pressure which is equal to partial pressure of A plus partial pressure of B this is the variation of p_A and this is the variation of partial pressure of component B. So, A is diffusing through this directions. So, this is the partial pressure distribution of A in non diffusing B.

(Refer Slide Time: 16:17)

Example 1 : Solution

Solution: CO₂ is diffusing through non diffusing air under steady state conditions at a total pressure of 1 atmosphere and temperature 300K. The partial pressure of CO₂ is 20kPa at one point and 5kPa at other point. The distance between the points is 5cm. Calculate the flux of CO₂. Given that at 300K and at 1 atm, D_{CO₂-air} = 2 x 10⁻⁵ m²/s.

Assume ideal gas
Let air = B

$$N_{CO_2} = \frac{D_{CO_2-air}}{RT(x_2 - x_1)} \times \frac{P_t}{P_{BLM}} (P_{CO_{2,1}} - P_{CO_{2,2}})$$

Given that $D_{CO_2-air} = 2 \times 10^{-5} \text{ m}^2/\text{s}$ at 300K and 1 atm. ✓

$P = 1 \text{ atm} = 101.3 \text{ kPa} = 1.013 \times 10^5 \text{ Pa}$

$T = 300 \text{ K}, x_2 - x_1 = 5 \text{ cm} = 0.05 \text{ m},$

$p_{CO_{2,1}} = 20 \text{ kPa} = 20,000 \text{ Pa}$ $P_{B,1} = P_t - P_{CO_{2,1}} = (101.3 - 20) \text{ kPa} = 81.3 \text{ kPa}$

$p_{CO_{2,2}} = 5 \text{ kPa} = 5,000 \text{ Pa}$ $P_{B,2} = P_t - P_{CO_{2,2}} = (101.3 - 5) \text{ kPa} = 96.3 \text{ kPa}$

$R = 8314 \text{ Pa m}^3/\text{kmol K}$

Now, let us take an example carbon dioxide is diffusing through non diffusing air under steady state conditions at a total pressure of one atmosphere and temperature of 300 Kelvin. The partial pressure of carbon dioxide is 20 kilo Pascal at one point and 5 kilo Pascal at other point the distance between the points is 5 centimeter. We need to calculate the flux of carbon dioxide given that at 300 Kelvin at and at 1 atmosphere pressure the diffusion coefficient of carbon dioxide in air is equal to 2 into 10 to the power minus 5 meter square per second.

Now, let us solve this we assume that it is ideal gas let air B the component B. So, we can write N_{CO_2} would be equal to D_{CO_2-air} divided by RT in into x_2 minus x_1 into P_t by P_{BLM} into partial pressure of CO_2 at 1 and partial pressure minus partial pressure of CO_2 at 2. So, this is D_{CO_2-air} is given 2 into 10 to the power minus 5 meter square per second at 300 Kelvin and 1 atmosphere pressure so that these data is given.

Now, P is the total pressure which is 1 atmosphere and if we just convert into kilo Pascal it would be 101.3 kilo Pascal which is equal to 1.01 into 10 to the power 5 Pascal. Now temperature is 300 Kelvin which is given x_2 minus x_1 the distance of diffusion is 5 centimeter. If we convert to meter it would be point 0.5 0.05 meter and then partial pressure of carbon dioxide at 0.1 is given 20 kilo Pascal which is 20000 Pascal partial

pressure of carbon dioxide at 0.2 is 5 kilo Pascal which is 5000 Pascal and R is given as 8314 Pascal meter cube per kilo mole Kelvin.

So, P B 1 would be equal to Pt minus P carbon dioxide at point 1 which would be equal to 101.3 minus 20 kilo Pascal which is around 81.3 kilo Pascal. And P B 2 you can calculate Pt minus P CO 2 at point 2 which is equal to 101.3 minus 5 kilo Pascal which is 96.3 kilo Pascal.

(Refer Slide Time: 19:41)

Example 1 : Solution

CO₂ is diffusing through non diffusing air under steady state conditions at a total pressure of 1 atmosphere and temperature 300K. The partial pressure of CO₂ is 20kPa at one point and 5kPa at other point. The distance between the points is 5cm. Calculate the flux of CO₂. Given that at 300K and at 1 atm, $D_{CO_2-air} = 2 \times 10^{-5} m^2/s$.

$P_{B,1} = P_t - P_{CO_2,1} = (101.3 - 20) kPa = 81.3 kPa$

$P_{B,2} = P_t - P_{CO_2,2} = (101.3 - 5) kPa = 96.3 kPa$

$$P_{BLM} = \frac{P_{B,2} - P_{B,1}}{\ln\left(\frac{P_{B,2}}{P_{B,1}}\right)} = \frac{96.3 - 81.3}{\ln\left(\frac{96.3}{81.3}\right)} kPa = 88.59 kPa = 88590 Pa$$

$$N_{CO_2} = \frac{2 \times 10^{-5} m^2/s \times 1.013 \times 10^5 Pa}{8314 Pa m^3/kmol K \times 300 K \times 0.05 m \times 88590 Pa} (20,000 - 5,000)$$

$$= \frac{2 \times 10^{-5} \times 1.013 \times 10^5 \times 15000}{8314 \times 300 \times 0.05 \times 88590} \frac{kmol}{m^2 s}$$

$$= 2.75 \times 10^{-6} \frac{kmol}{m^2 s}$$

So, this P B 1 and P B 2 are calculated, now if we calculate P B L M log mean partial pressure difference P B 2 minus P B 1 divided by ln P B 2 by P B 1 it would be equal to 96.3 minus 81.3 divided by ln to 96.3 divided by 81.3 kilo Pascal which is 88.59 kilo Pascal and which is equal to 88590 Pascal.

Now, we can calculate the flux NCO 2 would be equal to 2 into 10 to the power 5 meter square per second into 1.013 into 10 to the power 5 Pascal divided by 8314 Pascal meter cube per kilo mole Kelvin into 300 Kelvin is the temperature. And then distance is point not 5 meter into 88590 Pascal and the pressure differential is 20000 minus 5000 Pascal. So, it will lead to 2.75 into 10 to the power minus 6 kilo mole per meter square second.

(Refer Slide Time: 21:17)

Steady State Equimolar Counter Diffusion

This is the case for the diffusion of two ideal gases where an equal number of moles of the gases diffusing counter-current to each other.

- In this case $N_B = -N_A = \text{constant}$ and $N_A + N_B = 0$. ✓
- The molar flux equation (a) at steady state can then be written as:

$$N_A = -CD_{AB} \frac{dy_A}{dx} + y_A N$$

Where $N = N_A + N_B$

➔ $N_A = -CD_{AB} \frac{dy_A}{dx}$

Now, steady state equimolar counter diffusion this is the case for the diffusion of two ideal gases where an equal number of moles of the gases diffusing counter currently to each other. In this case N_B would be equal to minus N_A which is equal to constant. And so from this we can write $N_A + N_B$ is equal to 0. Now the molar flux in equation a at steady state can be written as this is equation 1 N_A is equal to minus $C D_{AB} \frac{dy_A}{dx} + y_A N$ and $N_A + N_B$ is equal to N which is 0. So, if we substitute that N is 0 we will get N_A is equal to minus $C D_{AB} \frac{dy_A}{dx}$.

(Refer Slide Time: 22:25)

Steady State Equimolar Counter Diffusion

For ideal gas $C = \frac{P_t}{RT}$

So, h

$$N_A = -\frac{D_{AB} P_t}{RT} \frac{dy_A}{dx}$$

Integrating the equation (h) with the boundary conditions: at $x = x_1, y_A = y_{A1}$; at $x = x_2, y_A = y_{A2}$, the equation of molar diffusion for steady-state equimolar counter diffusion can be represented as

$$N_A = \frac{D_{AB} P_t}{RT(x_2 - x_1)} (y_{A1} - y_{A2})$$

$$= \frac{D_{AB}}{RT(x_2 - x_1)} (P_1 - P_2)$$

Now, for ideal gas the concentration is equal to total pressure P_t divided by RT where R is the universal gas constant and T is the temperature. So, we can write N_A would be equal to $-\frac{dA B P_t}{RT} \frac{dy_A}{dx}$. Now if we integrate this relation with the boundary conditions at x_1 and y_{A1} and x_2 y_{A2} would be equal to y_{A2} .

The equation of molar diffusion for steady state equimolar counter diffusion can be represented as $N_A = \frac{D_{AB} P_t}{RT (x_2 - x_1)} \ln \frac{y_{A1} (1 - y_{A2})}{y_{A2} (1 - y_{A1})}$. So, from here if we rearrange it would be $D_{AB} \ln \frac{y_{A1} (1 - y_{A2})}{y_{A2} (1 - y_{A1})} = N_A (x_2 - x_1)$ into partial pressure of $P_{A1} - P_{A2}$ at point 2 is P_{A2} .

(Refer Slide Time: 23:49)

Example 2

CO_2 is diffusing at steady state through a straight tube of 0.5m long with an inside diameter of 0.05m containing N_2 at 300K and 1 atm pressure. The partial pressure of CO_2 at one end is 15kPa and 5kPa at the other end. Given that at 300K and 1atm. Given that $D_{\text{CO}_2-\text{N}_2} = 4 \times 10^{-5} \text{ m}^2/\text{s}$. Calculate the following for steady state equimolar counter diffusion:

- I. Molar flow rate of CO_2
- II. Molar flow rate of N_2

Now, let us consider another examples carbon dioxide is diffusing at steady state through a straight tube of 0.5 meter long with an inside diameter of point not 5 meter containing nitrogen at 300 Kelvin and 1 atmosphere pressure. The partial pressure of carbon dioxide at one end is 15 kilo Pascal and 5 kilo Pascal at the other end given that at 300 Kelvin and one atmosphere pressure the diffusion coefficient is $4 \times 10^{-5} \text{ m}^2/\text{s}$. Now, we need to calculate the following for the steady state equimolar counter diffusion the molar flow rate of carbon dioxide and the molar flow rate of nitrogen and we need to see whether they are equal or not.

(Refer Slide Time: 24:53)

Example 2 : Solution

Assume ideal gas in equimolar counter diffusion for CO₂ flux:

$$N_{CO_2} = \frac{D_{CO_2-N_2}}{RT(x_2 - x_1)}(p_{CO_2,1} - p_{CO_2,2})$$

Given

$$D_{CO_2-N_2} = 4 \times 10^{-5} m^2/s$$

$$P_t = 1 \text{ atm} = 101.3 \text{ kPa} = 1.013 \times 10^5 \text{ Pa}$$

$$T = 300 \text{ K}, x_2 - x_1 = 0.5m$$

$$p_{CO_2,1} = 15 \text{ kPa} = 15,000 \text{ Pa}$$

$$p_{CO_2,2} = 5 \text{ kPa} = 5,000 \text{ Pa} \checkmark$$

$$R = 8314 \text{ Pa m}^3/\text{kmol K}$$

So, we assume the ideal gas in equimolar counter diffusion for CO₂. So, the flux for CO₂ we can write N_{CO_2} would be equal to $D_{CO_2-N_2} / (RT(x_2 - x_1)) (p_{CO_2,1} - p_{CO_2,2})$. So, the value which are given $D_{CO_2-N_2}$ would be equal to $4 \times 10^{-5} m^2/s$. P_t is the total pressure 1 atmosphere which is equal to 101.3 kilo Pascal which is equal to 1.013×10^5 Pascal.

T is the temperature is 300 Kelvin and $x_2 - x_1$ is the distance of diffusion which is 0.5 meter partial pressure of CO₂ at one is 15 kilo Pascal which is 15000 Pascal and partial pressure of CO₂ at 0.2 is 5 kilo Pascal which is 5000 Pascal R is known 8314 Pascal meter cube per kilo mole Kelvin.

(Refer Slide Time: 26:15)

Example 2 : Solution

(i)
$$N_{CO_2} = \frac{D_{CO_2-N_2}}{RT(x_2 - x_1)}(p_{CO_2,1} - p_{CO_2,2})$$

$$= \frac{4 \times 10^{-5}}{8314 \times 300 \times 0.5} (15,000 - 5,000)$$

$$= \frac{0.4}{1247100} = 3.21 \times 10^{-7} \frac{kmol}{m^2s}$$

Cross sectional area of the tube:

$$A = \frac{\pi D_i^2}{4} = \frac{\pi}{4} \times (0.05)^2 = 1.96 \times 10^{-3} m^2$$

Molar flow rate of CO₂ = $3.21 \times 10^{-7} \frac{kmol}{m^2s} \times 1.96 \times 10^{-3} m^2 = 6.29 \times 10^{-10} \frac{kmol}{s}$

Now, molar flow rate of CO₂ = $N_{CO_2} \times A$

A = cross sectional area of the tube

Given that,
Internal diameter of the tube (D_i) = 0.05 m

So, N CO₂ if we substitute this parameters we will get 4 into 10 to the power minus 5 divided by 8314 into 300 into 0.5 into the partial pressure difference 15000 minus 5000. So, it will lead to 3.21 into 10 to the power minus 7 kilo mole per meter square second.

Now, the molar flow rate of carbon dioxide is equal to NCO₂ into the area A is the cross sectional area of the tube. So, given that internal diameter of the tube is D_i which is 0.05 meter. So, cross sectional area of the tube A is equal to pi D_i square by 4 which is equal to pi by 4 into 0.05 square which is equal to 1.96 into 10 to the power minus 3 meter square.

Now molar flow rate of carbon dioxide we can calculate which is equal to 3.21 into 10 to the power minus 7 kilo mole per meter square second which we have calculated flux into the cross sectional area 1.96 into 10 to the power minus 3 meter square which will give 6.29 into 10 to the power minus 10 kilo mole per second.

(Refer Slide Time: 27:49)

Example 2 : Solution

$$(ii) \quad N_{N_2} = \frac{D_{CO_2-N_2}}{RT(x_2-x_1)} (p_{N_2,1} - p_{N_2,2}) \quad \checkmark$$

Given

$$p_{N_2,1} = P_t - p_{CO_2,1} = (101.3 - 15)kPa = 86.3kPa = 86300 \text{ Pa} \quad \checkmark$$

$$p_{N_2,2} = P_t - p_{CO_2,2} = (101.3 - 5)kPa = 96.3kPa = 96300 \text{ Pa} \quad \checkmark$$

We know that for equimolar counter diffusion in ideal gases

$$D_{CO_2-N_2} = D_{N_2-CO_2}$$

$$\text{Or, } \frac{4 \times 10^{-5}}{8314 \times 300 \times 0.5} (86300 - 96300) = \frac{0.4}{1247100} = -3.21 \times 10^{-7} \frac{\text{kmol}}{\text{m}^2\text{s}}$$

$$\therefore \text{Molar flow rate of } N_2 = -3.21 \times 10^{-7} \frac{\text{kmol}}{\text{m}^2\text{s}} \times 1.96 \times 10^{-3} \text{ m}^2 = -6.29 \times 10^{-10} \frac{\text{kmol}}{\text{s}}$$

Now, let us calculate for nitrogen using the similar equations it is CO_2 N_2 by $RT \times 2$ minus x_1 into the partial pressure of N_2 at 1 minus partial pressure of N_2 at 0.2. So, the data for $P_{N_2,1}$ is P_t minus $P_{CO_2,1}$ which is equal to 101.3 minus 15 kilo Pascal. So, which is around 83.3 kilo Pascal so which is 86300 Pascal $P_{N_2,2}$ at 2 is equal to P_t minus $P_{CO_2,2}$ at 2 which is equal to 101.3 minus 5 kilo Pascal which is equal to 96.3 kilo Pascal which is equal to 96300 Pascal.

So, $P_{N_2,1}$ and $P_{N_2,2}$ is known now we know that for equimolar counter diffusion the diffusion coefficient of $D_{CO_2-N_2}$ would be equal to $D_{N_2-CO_2}$. Now if we substitute that we will obtain the flux is 3 minus 3.21 into 10 to the power minus 7 kilo mole per meter square second. So, the molar flow rate we can calculate using similar way minus 321 into 10 to the power minus 7 kilo mole per meter square second into 1.96 into 10 to the power minus 3 meter square which would be equal to minus 6.29 into 10 to the power minus 10 kilo mole per meter square second. So, this proves that the mutual diffusivities for the flux for both the components for equimolar counter diffusions are same.

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Non-Equimolar Counter Diffusion

In many situations, A and B molecules diffuse in opposite directions at different molar velocities.

Let us consider the following reaction , $2A+B=2C$

When one mole B diffuses towards A and two moles of A diffuse in opposite direction.

$$\text{Here, } N_A = -N_B / 2$$

For non equimolar counter diffusion in many situation A and B molecules diffuse in opposite directions at different molar velocities like let us consider the following reactions. We can consider 2 A plus B is equal to 2 C. So, in this case when one mole of B diffuses towards A and two moles of A diffuse in opposite direction we can write N_A is equal to minus N_B by 2. So, from these we can calculate the flux of different components using this relations. So, thank you for hearing this lectures and in the next lecture we will discuss on the diffusion mass transfer for non uniform geometries.

Thank you very much.