

**M.Sc. DEGREE EXAMINATION, NOVEMBER 2018**  
**I Year I Semester**  
**Core Elective -I**  
**PROBABILITY AND DISTRIBUTIONS**

**Time : 3 Hours**

**Max.marks :75**

**Section A** ( $10 \times 2 = 20$ ) Marks

Answer any **TEN** questions

1. Write the mean and variance of negative Binomial distribution
2. Obtain the moment generating function of Uniform distribution.
3. If  $f(x, y) = e^{-(x+y)}$ ;  $0 < x < 8$ ,  $0 < y < 8$ , obtain the distribution function of  $(X, Y)$
4. Define Conditional variance.
5. Define Bivariate normal distribution.
6. Write the probability function of bivariate Poisson distribution.
7. Write the mgf of Chi-square distribution.
8. Define T-Statistic.
9. Write the mean and variance of F distribution.
10. Define convergence in probability.
11. Give two examples of stable distribution.
12. Define moment generating function of  $(X, Y)$ .

**Section B** ( $5 \times 5 = 25$ ) Marks

Answer any **FIVE** questions

13. Obtain the moment generating function of multinomial distribution.
14. Establish the additive property of normal distribution.
15. If  $X_1, X_2$  and  $X_3$  be iid random variables with  $f(x) = \begin{cases} e^{-x}, & x > 0 \\ 0, & \text{otherwise} \end{cases}$

then show that  $Y_1 = X_1 + X_2 + X_3$ ,  $Y_2 = \frac{X_1 + X_2}{X_1 + X_2 + X_3}$  and  $Y_3 = \frac{X_1}{X_1 + X_2}$  are independent.

16. If  $X$  and  $Y$  are jointly distributed with density function  
 $f(x, y) = e^{-x-y}$ ,  $0 < x < 8$ ,  $0 < y < 8$ , show that  $X$  and  $Y$  are independent
17. Obtain mean and variance of bivariate Poisson distribution.
18. Establish the relationship between  $t$  and  $F$ .
19. Define (i) convergence in distribution (ii) convergence in  $r$ th moment  
(iii) convergence almost surely.

**Section C** ( $3 \times 10 = 30$ ) Marks

Answer any **THREE** questions

20. Obtain mean, median and mode of normal distribution.
21. (i) Define bivariate moment generating function (ii) For a positive random variable with finite first moment show that (a)  $E\sqrt{x} \leq \sqrt{EX}$  and  
(b)  $E[1/X] \geq 1/EX$
22. If  $(X, Y)$  has a bivariate normal distribution, show that  $X$  and  $Y$  are independent if and only if  $\rho = 0$
23. If  $X$  follows Chi-square distribution with  $n$  d.f then S.T.  $\lim$   
$$P\{\sqrt{2X} - \sqrt{2n-1} \leq z\} = \int_{-\infty}^{\infty} \frac{1}{\sqrt{2\pi}} e^{-y^2/2} dy$$
24. State and prove Lindeberg-Levy Central Limit theorem.

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