

**B.Sc. DEGREE EXAMINATION, NOVEMBER 2018**  
**III Year V Semester**  
**Core Elective - Paper I**  
**NUMERICAL METHODS**

**Time : 3 Hours**

**Max.marks :75**

**Section A** ( $10 \times 2 = 20$ ) Marks

Answer any **TEN** questions

1. Write Newton-Raphson formula.
2. Define absolute error and relative error.
3. State one direct method and iterative method for solving system of linear equations.
4. When a matrix is said to be diagonally dominant?
5. Write Lagrange's Interpolation formula.
6. Find the divided difference table for the function  $f(x) = x^2 + 2x + 2$  whose arguments are 1, 2, 4, 7, 10.
7. Write Newton-cote's quadrature formula.
8. Write the truncation error in Simpson's 1/3rd rule.
9. Solve  $y' = 1 - y$ ,  $y(0) = 0$  find  $y$  at  $x = 0.1$  using Euler's method.
10. Write Adams-Bashforth predictor and corrector formula.
11. Find the value of  $x$  when  $y = 7$  from the following data

X	1	3	4
Y	4	12	19

12. Prove that  $\delta = E^{1/2} - E^{-1/2}$

**Section B** ( $5 \times 5 = 25$ ) Marks

Answer any **FIVE** questions

13. Use the method of iteration solve  $3x - \log_{10} x = 6$
14. Solve the system of equations by Gauss Elimination method  
 $x + y + z = 9$   
 $2x - 3y + 4z = 13$   
 $3x + 4y + 5z = 40$
15. Find the value of  $y$  when  $x = 9$  using Newton's divided difference method from the following data

X	5	7	11	13	17
Y	150	392	1452	2366	5202

16. Find  $y'(x)$  at  $x = 0.5$  from the following data

X	0	1	2	3	4
Y	1	1	15	40	85

17. Find an approximate solution of the initial value problem  $y' = 1 + y^2$ ,  $y(0) = 0$  by Picard's method and compare with the exact solution.
18. Find  $\Delta^n \sin x$  taking  $h = 1$ .
19. Find the real root of the equation  $x^3 - 3x + 1 = 0$  using Regula-Falsi method.

### Section C ( $3 \times 10 = 30$ ) Marks

Answer any **THREE** questions

20. Find the real root of the equation  $x^3 - x - 11 = 0$  using bisection method.

21. Solve the system of equations by Gauss-Seidel method

$$6x + 15y + 2z = 72$$

$$x + y + 54z = 110$$

$$27x + 6y - z = 85$$

22. Find the value of  $y$  when  $x = 48$  and  $x = 84$  from the following data

X	40	50	60	70	80	90
Y	184	204	226	250	276	304

23. Evaluate  $\int_0^1 \frac{dx}{1+x}$ ,  $h = \frac{1}{6}$  using (i) Trapezoidal rule (ii) Simpson's 1/3rd rule (iii) Simpson's 3/8th rule
24. Compute  $y(0.1)$ ,  $y(0.2)$  by Runge-kutta method of order four for the differential equation  $y' = xy + y^2$ ,  $y(0) = 1$ .

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