B.Sc. DEGREE EXAMINATION,NOVEMBER 2018 II Year III Semester Allied-Paper MATHEMATICAL STATISTICS-I

Time : 3 Hours

Max.marks:75

Section A $(10 \times 2 = 20)$ Marks

Answer any **TEN** questions

- 1. Define trial.
- 2. Define equally likely events.
- 3. Define discrete random variable?
- 4. Write the properties of distribution.
- 5. If C is a constant and Y=H(X) is a random variable then E(C.H(X))=C.E(H(X))
- 6. Define r^{th} moment about the origin.
- 7. Write any two examples of Bernoulli trials.
- 8. Write the mean and variance of normal distribution .
- 9. Write the MGF of gamma distribution.
- 10. Write the definition of beta distribution of first kind.
- 11. Define independent events.
- 12. Define poisson distribution.

Section B $(5 \times 5 = 25)$ Marks

Answer any **FIVE** questions

- 13. A coin is tossed twice. Find the probability of getting atleast one head.
- 14. Explain cumulative probability distribution function.
- 15. Find the mathematical expectation of the product of the points on n dice.
- 16. Find the rth moment about the origin, the mean and the standard deviation of the distribution whose p.d.f is given by

$$f(x) = \begin{cases} 2(1-x) & for \quad 0 < x < 1\\ 0, otherwise \end{cases}$$

- 17. Derive the mean of gamma distribution.
- 18. An integer is chosen at random out of the integers from 1 to 100. What is the probability that it is (i) multiple of 5 and (ii) divisible by 7.
- 19. Write the properties of normal distribution.

Section C $(3 \times 10 = 30)$ Marks

Answer any **THREE** questions

- 20. A company has three machines M_1 , M_2 , M_3 which produces 20%, 30% and 50% of the products respectively. Their respective defective percentages are 7, 3 and 5. From these products one is chosen and inspected. It is defective. What is the probability that is has been made by machine M_3 .
- 21. A continuous random variable x has the following pdf

$$f(x) = \begin{cases} 3x^2 & for \quad 0 < x < 1\\ 0, otherwise \end{cases}$$

Verify that it is a pdf and evaluate the following probabilities.

(i)
$$P\left(X \le \frac{1}{3}\right)$$
, (ii) $P\left(\frac{1}{3} \le X \le \frac{1}{2}\right)$

- 22. If X and Y are independent random variables defined on a sample space S then E(XY)=E(X)E(Y)
- 23. Derive the mode of binomial distribution.
- 24. Derive the mean and variance of Uniform distribution.

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