M.Sc DEGREE EXAMINATION, APRIL 2019 I Year I Semester Probability and Distribution Theory

Time : 3 Hours

Max.marks:75

Section A $(10 \times 2 = 20)$ Marks

Answer any **TEN** questions

- 1. Define Sample Space.
- 2. Define conditional probability.
- 3. What do you mean by random variables?
- 4. Define the probability mass function.
- 5. Define a negative binomial distribution.
- 6. What do you mean by Poisson random variable?
- 7. Define a hyper-geometric random variable.
- 8. Define a Multinomial distribution.
- 9. State bivariate poisson distribution.
- 10. Define bivariate continuous distribution.
- 11. Define a bivariate normal distribution.
- 12. State Multivariate normal distribution.

Section B $(5 \times 5 = 25)$ Marks

Answer any **FIVE** questions

- 13. State and prove multiplication rule for probability.
- 14. A card is chosen at random from a deck of 52 cards. Let A be the event that the card is an ace, and B, the event that it is a club then prove that A and B are independent.
- 15. Find Mean and variance of hyper-geometric distribution.
- 16. Prove that the correlation coefficient ρ between two random variables X and Y satisfies $|\rho| = 1$.
- 17. If $Ex^2 < \alpha$ then prove that $Var(x) = Var(E{XIY}) + E(Var{XIY})$
- 18. Find Mean and variance of bivariate binomial distribution.
- 19. Find Moment generating function of a multinomial distribution.

Section C $(3 \times 10 = 30)$ Marks

Answer any **THREE** questions

- 20. State and prove Bayes' theorem.
- 21. Let Eh(x) exists then prove that $Eh(x) = E\{E(h(x)) | Y\}$
- 22. Find the Mean and variance of a Gamma distribution.
- 23. Find the Mean and variance of a Multinomial distribution.
- 24. Prove that if (x,y) has a bivariate normal distribution, X and Y are independent if and only if $\rho = 0$.

M.Sc DEGREE EXAMINATION, APRIL 2019 I Year I Semester Probability and Distribution Theory

Time : 3 Hours

Max.marks:75

Section A $(10 \times 2 = 20)$ Marks

Answer any **TEN** questions

- 1. Define Sample Space.
- 2. Define conditional probability.
- 3. What do you mean by random variables?
- 4. Define the probability mass function.
- 5. Define a negative binomial distribution.
- 6. What do you mean by Poisson random variable?
- 7. Define a hyper-geometric random variable.
- 8. Define a Multinomial distribution.
- 9. State bivariate poisson distribution.
- 10. Define bivariate continuous distribution.
- 11. Define a bivariate normal distribution.
- 12. State Multivariate normal distribution.

Section B $(5 \times 5 = 25)$ Marks

Answer any **FIVE** questions

- 13. State and prove multiplication rule for probability.
- 14. A card is chosen at random from a deck of 52 cards. Let A be the event that the card is an ace, and B, the event that it is a club then prove that A and B are independent.
- 15. Find Mean and variance of hyper-geometric distribution.
- 16. Prove that the correlation coefficient ρ between two random variables X and Y satisfies $|\rho| = 1$.
- 17. If $Ex^2 < \alpha$ then prove that $Var(x) = Var(E{XIY}) + E(Var{XIY})$
- 18. Find Mean and variance of bivariate binomial distribution.
- 19. Find Moment generating function of a multinomial distribution.

Section C $(3 \times 10 = 30)$ Marks

Answer any **THREE** questions

- 20. State and prove Bayes' theorem.
- 21. Let Eh(x) exists then prove that $Eh(x) = E\{E(h(x)) | Y\}$
- 22. Find the Mean and variance of a Gamma distribution.
- 23. Find the Mean and variance of a Multinomial distribution.
- 24. Prove that if (x,y) has a bivariate normal distribution, X and Y are independent if and only if $\rho = 0$.