

**B.Sc. DEGREE EXAMINATION, APRIL 2019**  
**III Year VI Semester**  
**FORMAL LANGUAGES AND AUTOMATA THEORY**

**Time : 3 Hours**

**Max.marks :75**

**Section A** ( $10 \times 2 = 20$ ) Marks

Answer any **TEN** questions

1. Define Context - sensitive language
2. Define Context free grammar.
3. Define the union and product of  $L_1$  and  $L_2$ .
4. Define reversal or reflection.
5. Define word or string or sentence and give examples.
6. Define phrase structure language.
7. Define transition diagram.
8. Define regular set.
9. State Ogden's Lemma
10. Define regular expression.
11. Define finite control.
12. Prove that  $n$  is no greater than the number of states of the smallest FA accepting  $L$ .

**Section B** ( $5 \times 5 = 25$ ) Marks

Answer any **FIVE** questions

13. Construct context – free grammar to generate a context free language where  $N = \{S\}$ ,  $T = \{a,b\}$  and  $P = S \rightarrow aSb$  and  $S \rightarrow ab$ .
14. Prove that every context sensitive language is generated by a context sensitive
15. Construct context – sensitive grammar to generate a context sensitive language. Let  $G = (N, T, P, S)$  where  $N = \{S, B\}$ ,  $T = \{a,b,c\}$  and  $P = S \rightarrow aSBc$ ,  $S \rightarrow abc$ ,  $cB \rightarrow Bc$ ,  $Bb \rightarrow bb$ .
16. Show that  $L$  be a set accepted by a nondeterministic finite automaton then there exists a deterministic finite automaton that accepts  $L$ .
17. Show that  $r$  be a regular expression then there exist an NFA with  $\epsilon$  - transitions that accepts  $L(r)$

18. State any two applications of pumping lemma.
19. State the pumping lemma for the CFL

**Section C** ( $3 \times 10 = 30$ ) Marks

Answer any **THREE** questions

20. Let  $L = \{w/w \text{ is in } \{a,b\}^+ \text{ and } w \text{ consists of an even number of } a\text{'s and an even number of } b\text{'s}\}$  generate the regular grammar and give reason.
21. Prove that the families of PSL, CSL, CFL and RL are closed under product.
22. Let  $L = \{w/w \text{ is in } \{a,b\}^+ \text{ and } w \text{ does not contain two consecutive } a\text{'s}\}$  generate the regular grammar and give reason.
23. Prove that equivalence of NFA's with and without  $\epsilon$  - moves.
24. State and prove Ogden's Lemma.

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