

B.Sc DEGREE EXAMINATION, APRIL 2019
I Year II Semester
Allied Mathematics-II

Time : 3 Hours

Max.marks :75

Section A ($10 \times 2 = 20$) Marks

Answer any **TEN** questions

1. Define Bisection method.
2. State Regula -Falsi formula.
3. Prove that $E = 1 + \Delta$.
4. State Newton's backward interpolation formula for equal intervals.
5. From the following table find $f(0)$ using Newton's divided difference interpolation formula:

$x:$	-1	1	2	3
$f(x):$	-21	15	12	3
6. State Lagrange's inverse interpolation formula.
7. State Newton's backward difference formula to compute first and second derivatives.
8. What is Simpson's three-eighth formula ?
9. Find $y(0.01)$ if $\frac{dy}{dx} = -y$, $y(0) = 1$ by Euler's method.
10. Write down the Runge-Kutta formula of fourth order to solve $\frac{dy}{dx} = f(x, y)$ with $y(x_0) = y_0$.
11. Find the sixth term of the sequence 8, 12, 19, 29, 42, ...
12. Obtain the divided difference table for

$x :$	0	2	3	4	7
$f(x) :$	4	23	58	112	466

Section B ($5 \times 5 = 25$) Marks

Answer any **FIVE** questions

13. Find the real root of the equation $x^3 - 10x - 5 = 0$ by iteration method
14. Find $f(x)$ and $f(0.5)$ of the following table

$x :$	0	1	2	3	4	5	6
$f(x):$	-1	3	19	53	111	199	323

15. From the following table find $f'(5)$ using Newton's interpolation formula.

$x :$	0	1	3	6
$f(x) :$	1	4	88	1309

16. Evaluate $\int_0^1 \frac{x^2}{1+x^3} dx$ using Simpson's one-third rule with $h = 0.25$.

17. Solve numerically $\frac{dy}{dx} = x + y$, $y(0) = 1$ for $x = 0.2, 0.4, 0.6, 0.8, 1.0$ by Euler's method.

18. Find the positive root of $x^3 - 5x + 3 = 0$ by Newton-Raphson method correct to three decimal places.

19. Using Taylor series method find $y(1.1)$ given $\frac{dy}{dx} = x + y$, $y(1) = 0$.

Section C ($3 \times 10 = 30$) Marks

Answer any **THREE** questions

20. Find a real root of the equation $x^3 - 5x - 7 = 0$ using Regula-Falsi method.

21. Use Newton's formula for interpolation to find the net premium at age 25 from the table given below.

Age:	20	24	28	32
Annual Premium:	0.01427	0.01581	0.01772	0.01996

22. Using Lagrange's interpolation formula, find the value of y when $x = 10$ for following data.

$x:$	5	6	9	11
$y:$	12	13	14	16

23. Find the second derivatives of $f(x)$ at $x = 2.96$ at by Newton's forward formula from the following data.

$x :$	2.94	2.96	2.98	3.00	3.02	3.04	3.06
$f(x) :$	0.1826	0.1811	0.1797	0.1783	0.1769	0.1755	0.1742

24. Using Runge-Kutta method of fourth order, find $y(0.8)$ correct to 4 decimal places if $\frac{dy}{dx} = y - x^2$, $y(0.6) = 1.7379$, taking $h = 0.1$

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