

M.Sc. DEGREE EXAMINATION, NOVEMBER 2019
I Year II Semester
Topology

Time : 3 Hours

Max.marks :75

Section A ($10 \times 2 = 20$) Marks

Answer any **TEN** questions

1. Give an example of a complete metric space which is not complete.
2. Define a norm on the linear space R^n .
3. Define an open base for a topological space.
4. Define a topological space.
5. Define locally compact space.
6. Define an lebesgue number for an open cover of X .
7. Show that every totally bounded space is bounded.
8. State the Bolzano-weierstrass property.
9. Define a T_1 topological space.
10. Give an example of a Hausdorff space.
11. Define a normal space.
12. State Urysonh's Lemma.

Section B ($5 \times 5 = 25$) Marks

Answer any **FIVE** questions

13. Let X and Y be metric spaces. Show that a map $f : X \rightarrow Y$ is continuous if and only if $f^{-1}(G)$ is open in X whenever G is open in Y .
14. Let X be a topological space and A a subset of X , show that $\overline{A} = A \cup D(A)$. Deduce that A is closed if and only if $A \supseteq D(A)$.
15. Prove that any continuous image of a compact space is compact.
16. Prove that the product of any non-empty class of Hausdorff spaces is Hausdorff space.
17. Prove that the components of a totally disconnected space are its points.
18. Show that every compact Hausdorff is normal.
19. Let X be a topological space and A be a subset of X . Prove that $\overline{A} = \{x : \text{each neighbourhood of } x \text{ intersects } A\}$.

Section C ($3 \times 10 = 30$) MarksAnswer any **THREE** questions

20. Prove that the set R^n of all n- tuples $X = (x_1, x_2, \dots, x_n)$ of real numbers is a real Banach space.
21. Prove that every separable metric space is second countable.
22. State and prove Tychonoff's theorem.
23. State and prove Tietze extension theorem.
24. Prove that a subspace of the real line R is connected if and only if it is an interval.

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