

**M.Sc. DEGREE EXAMINATION, ODD SEMESTER 2020**  
**II Year III Semester**  
**Complex Analysis**

**Max.marks :25**

Answer any **FIVE** questions ( $5 \times 5 = 25$ ) Marks

1. State and prove Liouville's theorem.
2. Let  $G$  be a region in  $\mathbb{C}$  and  $f$  an analytic on  $G$ . Suppose there is a constant  $M$  such that  $\lim_{z \rightarrow a} \sup |f(z)| \leq M$  for all  $a$  in  $G$ . Prove that  $|f(z)| \leq M$  for all  $z$  in  $G$ .
3. Let  $\operatorname{Re} Z_n \geq -1$  then prove that the series  $\sum \log(1 + Z_n)$  converges absolutely iff the  $\sum Z_n$  converges absolutely.
4. State and prove mean value theorem.
5. State and prove little Picard theorem.
6. State and prove Morera's theorem.
7. State and prove Euler's theorem of sequence of prime numbers.