

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN  
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)  
Chromepet, Chennai — 600 044.

B.Sc. END SEMESTER EXAMINATIONS APRIL-2022

SEMESTER - IV

20USTAT4004 - Numerical Methods

Total Duration : 3 Hrs.

Total Marks : 60

**Section A**

Answer any **SIX** questions ( $6 \times 5 = 30$  Marks)

1. Derive Gregory-Newton's backward interpolation formula.
2. Derive Newton's divided difference formula .
3. Derive Gauss's forward formula.
4. Find by Newton Raphson's method a real root of  $3x - \cos x - 1 = 0$
5. Evaluate  $\int_0^{\frac{\pi}{3}} \sqrt{\sin x} dx$  with  $n = 6$  using Simpson's method.
6. Find root of equation  $x^3 - 4x - 9 = 0$  .
7. Construct a forward differences table for the following values of  $x$  and  $y$

|   |        |        |        |        |        |        |        |
|---|--------|--------|--------|--------|--------|--------|--------|
| x | 35     | 36     | 37     | 38     | 39     | 40     | 41     |
| y | 14.298 | 14.144 | 13.986 | 13.825 | 13.661 | 13.495 | 13.328 |

8. Apply Bessel's formula to obtain  $f(32)$  given that  $f(25)=0.2707$ ,  $f(30)=0.3027$ ,  $f(35)=0.3388$ ,  $f(40)=0.3794$ .

**Section B**

Answer any **THREE** questions ( $3 \times 10 = 30$  Marks)

9. Find the interpolating polynomial  $f(x)$  satisfying  $f(0)=0$ ,  $f(2)=4$ ,  $f(4)=56$ ,  $f(6)=204$ ,  $f(8)=496$  and  $f(10)=980$  and hence find  $f(3)$ ,  $f(5)$ .
10. Apply Lagrange's formula to find  $f(5)$  and  $f(6)$  gives that  $f(1)=2$ ,  $f(2)=4$ ,  $f(3)=8$ ,  $f(4)=16$  and  $f(7)=128$ .
11. Derive Stirling's Central difference formula.
12. Solve the following system of equation Gauss-Seidel method correct to three decimal places.  $x+y+54z=110$ ;  $27x+6y-z=85$ ;  $6x+15y+2z=72$ .
13. Evaluate the integral  $I = \int_0^1 \frac{dx}{\sqrt{1+x^2}}$  by trapezoidal rule dividing the integral  $[0,1]$  into 5 equal parts. Compute up to 3 decimals.

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