

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN  
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)  
Chromepet, Chennai — 600 044.

M.Sc. - END SEMESTER EXAMINATIONS APRIL - 2022

SEMESTER - I

08PPHCT1001 - Mathematical Physics

Total Duration : 3 Hrs.

Total Marks : 60

**Section A**

Answer any **SIX** questions ( $6 \times 5 = 30$  Marks)

1. Show that the vectors  $(1,2,-3), (1,3,-2)$  and  $(2,-1,5)$  are linearly independent
2. Prove that  $P_2 m(0) = (-1)^m \frac{2m!}{2^{2m} 2m!^2}$
3. Determine the analytic function whose real part is  $x^3 - 3xy^2 + 3x^2 + 1$
4. Find the fourier series of the function  $e^x$  in the interval  $-\pi < x < \pi$ .
5. Explain the construction of  $C_{4V}$  character table
6. S.T. (i)  $H_{2n}(0) = (-1)^n \frac{n^{2n}}{n!}$  (ii)  $H_{2n+1}(0) = 0$
7. Find the residue of  $\frac{Ze^{iz}}{a^4 + z^4}$  at its poles
8. Find the Laplace transform of the sawtooth wave function  $f(t) = \frac{at}{T}$   $0 < t < T$  and  $f(t+T)=f(t)$

**Section B**

**Part A**

Answer any **TWO** questions ( $2 \times 10 = 20$  Marks)

9. Explain Schmidt orthogonalization method
10. Show that  $\int_{-1}^{+1} P_m(x) P_n(x) dx = \frac{2}{2n+1} \delta_{mn}$
11. Apply calculus of residues to show that  $\int_0^\infty \frac{dx}{(x^2 + 1)(x^2 + 4)} = \frac{\pi}{24}$
12. Explain great orthogonality theorem

**Part B**

Compulsory question ( $1 \times 10 = 10$  Marks)

13. Show that a periodic function  $f(x)$  can be expressed as Fourier series. Derive the expression for coefficients  $a_0, a_n, b_n$

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