

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)
Chromepet, Chennai — 600 044.

B.Sc. END SEMESTER EXAMINATIONS APRIL-2022

SEMESTER - I

08UMACT1001 & UMA/CT/1001 - Trigonometry and Analytical Geometry of Two dimensions

Total Duration : 3 Hrs.

Total Marks : 60

Section A

Answer any **SIX** questions ($6 \times 5 = 30$ Marks)

1. Expand $\cos 6\theta$ in terms of $\sin \theta$.
2. Separate real and imaginary parts of $\tan^{-1}(x+iy)$.
3. Prove that, $i^i = e^{-(4n+1)\frac{\pi}{2}}$
4. Find the sum to infinity of the series $c \cos \alpha - \frac{c^3}{3} \cos 3\alpha + \frac{c^5}{5} \cos 5\alpha - \dots$
5. Find the polar of the point (x_1, y_1) with respect to the parabola $y^2 = 4ax$.
6. Expand $\sin^7 \theta$ in a series of sines of multiples of θ .
7. Show that, $\tanh^{-1} x = \frac{1}{2} \log_e \left(\frac{1+x}{1-x} \right)$.
8. Find the sum to infinity of the series $c \sin \alpha + \frac{c^2}{2!} \sin 2\alpha + \frac{c^3}{3!} \sin 3\alpha + \dots$

Section B

Answer any **THREE** questions ($3 \times 10 = 30$ Marks)

9. Show that, $\frac{\sin 6\theta}{\sin \theta} = 32 \cos^5 \theta - 32 \cos^3 \theta + 6 \cos \theta$.
10. If $u = \log \tan \left(\frac{\pi}{4} + \frac{\theta}{2} \right)$, then show that $\tanh \frac{u}{2} = \tan \frac{\theta}{2}$ and $\theta = -i \log \tan \left(\frac{\pi}{4} + i \frac{u}{2} \right)$.
11. If $\log \sin(\theta + i\varphi) = A + iB$, then show that
 - (i) $2e^{2A} = \cosh 2\varphi - \cos 2\theta$
 - (ii) $\cos(\theta - B) = e^{2\varphi} \cos(\theta + B)$
12. Find the sum to infinity of the series
$$\cos \alpha + \frac{1}{2} \cos(\alpha + \beta) + \frac{1.3}{2.4} \cos(\alpha + 2\beta) + \frac{1.3.5}{2.4.6} \cos(\alpha + 3\beta) \dots$$
13. Find the pole of the line $lx + my + n = 0$ with respect to the ellipse
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1.$$
