

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN  
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)  
Chromepet, Chennai — 600 044.

B.Sc. END SEMESTER EXAMINATIONS APRIL-2022

SEMESTER - V

17UMACE5A01 - Numerical Methods

Total Duration : 3 Hrs.

Total Marks : 60

**Section A**

Answer any **SIX** questions ( $6 \times 5 = 30$  Marks)

1. Evaluate  $\sqrt{12}$  by using Newton Raphson method correct to 3 decimal places.
2. Solve the system of equations by Guass elimination method.  
 $x+2y+z=3$ ,  $2x+3y+3z=10$ ,  $3x-y+2z=13$ .
3. Find the function  $f(x)$  from the following table hence evaluate  $f(6)$  by Newton's method.

|      |   |   |   |   |
|------|---|---|---|---|
| x    | 1 | 2 | 7 | 8 |
| f(x) | 1 | 5 | 5 | 4 |

4. Evaluate  $I = \int_0^6 \frac{1}{1+x} dx$  using (i) Trapezoidal rule (ii) Simpson's one-third rule
5. Using Euler's method , Solve numerically the equation,  $y' = x+y$ ,  $y(0)=1$ , for  $x=(0.0),(0.2),(1.0)$ .
6. Find the positive root of  $X^3 - X = 1$  correct to four decimal places by bijection method.
7. Solve the system of equations by Guasseidal method.  
 $10x+2y+z=13$ ,  $x+10y-2z=9$ ,  $3x-y+10z=12$ .
8. Using Lagrange's interpolation formula find  $y(10)$  from the following table.

|   |    |    |    |    |
|---|----|----|----|----|
| X | 5  | 6  | 9  | 11 |
| Y | 12 | 13 | 14 | 16 |

**Section B**

Answer any **THREE** questions ( $3 \times 10 = 30$  Marks)

9. Find a positive root of  $x-\cos x = 0$  by Regula falsi method correct to four decimal places.
10. Apply Guass forward formula to obtain  $f(x)$  at  $x=3.5$  from the table below.

|      |       |       |       |       |
|------|-------|-------|-------|-------|
| x    | 2     | 3     | 4     | 5     |
| f(x) | 2.626 | 3.454 | 4.784 | 6.986 |

Contd...

11. From the data given below, find the value of  $x$  when  $y=13.5$  .

|     |       |       |       |       |       |
|-----|-------|-------|-------|-------|-------|
| $x$ | 93.0  | 96.2  | 100.0 | 104.2 | 108.7 |
| $y$ | 11.38 | 12.80 | 14.70 | 17.07 | 19.91 |

12. The population of a certain town is given below. Find the rate of growth of the population in 1931, 1941, 1961 and 1971.

|                         |     |       |       |       |        |        |
|-------------------------|-----|-------|-------|-------|--------|--------|
| Year                    | $x$ | 1931  | 1941  | 1951  | 1961   | 1971   |
| Population in thousands | $y$ | 40.62 | 60.80 | 79.95 | 103.56 | 132.65 |

13. Obtain the values of  $y$  at  $x=0.1, 0.2$ . Using Runge Kutta fourth order for the differential equation  $y'=-y$ , given  $y(0)=1$ .

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