SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai — 600 044. B.Sc. END SEMESTER EXAMINATIONS APRIL-2022 SEMESTER - IV 20UMAAT4004 - Mathematical Statistics - II

Total Duration : 3 Hrs.

Total Marks : 60

Section A

Answer any **SIX** questions $(6 \times 5 = 30 \text{ Marks})$

- 1. Derive the additive property of X^2 variates.
- 2. If T is an unbiased estimator for θ , show that T² is a biased estimator for θ^2 .
- 3. Define Consistency and Efficiency.
- 4. Explain Maximum Likelihood estimator.
- 5. Explain Method of moments.
- 6. Define Null Hypothesis Alternate hypothesis.
- 7. Explain Type I error and Type II error.
- 8. Explain Chi square test of Goodness of fit.

Section B

Answer any **THREE** questions $(3 \times 10 = 30 \text{ Marks})$

- 9. Derive Student's t distribution.
- 10. State and prove Cramer Rao inequality.
- 11. Obtain $100(1-\alpha)$ % confidence intervals for the parameter θ of the normal

distribution
$$f(x,\theta;\sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left[-\frac{1}{2}\left(\frac{x-\theta}{\sigma}\right)^2\right]$$
, $-\infty < x < \infty$.

- 12. Explain the procedure for testing of hypothesis.
- 13. Describe the χ^2 test for independence of attributes.
