SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai — 600 044. B.Sc. END SEMESTER EXAMINATIONS APRIL-2022 SEMESTER - I 16UMACT1A02 & UMA/CT/1A02 - Differential Calculus

Total Duration : 3 Hrs.

Total Marks : 60

Section A

Answer any **SIX** questions $(6 \times 5 = 30 \text{ Marks})$

1. Find the nth derivative of $e^{3x} \sin x \sin 2x \sin 3x$.

2. If x+y+z=u, y+z=uv, z=uvw, then show that, $\frac{\partial(x,y,z)}{\partial(u,v,w)}=u^2v$.

- 3. Find the radius of curvature of the curve $x^4+y^4 = 2$ at the point (1,1).
- 4. Show that, the p-r equation of the cardioid $r = a(1-\cos\theta)$ is $p^2 = \frac{r^3}{2a}$.
- 5. Find the asymptotes of $x^3+2x^2y-xy^2-2y^3+4y^2+2xy+y-1=0$.
- 6. Find y_n where $y = \frac{3}{(x+1)(2x-1)}$.
- 7. Find the minimum value of $x^2+5y^2-6x+10y+12$.
- 8. Find the radius of curvature of the curve $r^2 = a^2 \sin 2\theta$.

Section B

Answer any **THREE** questions $(3 \times 10 = 30 \text{ Marks})$

- 9. If $y = e^{a \sin^{-1}x}$ then show that, (1- x^2) $y_2 xy_1 a^2y = 0$ and hence show that, (1- x^2) $y_{n+2} (2n+1) xy_{n+1} (n^2+a^2) y_n = 0$.
- 10. If $u = a^3x^2 + b^3y^2 + c^3z^2$ and $\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 1$, then find the minimum value of u.
- 11. Show that, the radius of curvature at a point $(a\cos^3\theta, a\sin^3\theta)$ on the curve $x^{2/3} + y^{2/3} = a^{2/3}$ is $3a\sin\theta\cos\theta$.
- 12. Derive the radius of curvature in polar coordinates.
- 13. Show that, the asymptotes of the cubic $x^2 y xy^2 + xy + y^2 + x y = 0$ cut the curve again in three points which lie on the line x + y = 0.
