

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN  
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)

Chromepet, Chennai — 600 044.

B.Sc.(Chemistry) - END SEMESTER EXAMINATIONS APRIL-2023

SEMESTER - II

**20UCHAT2002 - Allied Mathematics II**

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

### Section B

Answer any **SIX** questions ( $6 \times 5 = 30$  Marks)

1. Determine the Fourier series for  $f(x) = \left(\frac{\pi - x}{2}\right)$  in  $[-\pi, \pi]$ .
2. Find the Laplace transform of  $t \cos^2 t$ .
3. Evaluate  $L^{-1} \left[ \frac{4s + 5}{(s - 1)^2(s + 2)} \right]$
4. Determine curl F if  $F = x^2 y \bar{i} + y^2 z \bar{j} + z^2 x \bar{k}$ .
5. Eliminate the arbitrary function f from  $f(xy + z^2, x + y + z) = 0$ .
6. Find the Laplace transform of  $\frac{\sin at}{t}$ .
7. Determine the inverse Laplace of  $\frac{a + bs}{s^3}$ .
8. Determine  $\oint_C x dx + y dy$ , where C is the ellipse  $x^2 + 4y^2 = 4$ .

### Section C

Answer any **THREE** questions ( $3 \times 10 = 30$  Marks)

9. Determine the fourier series for  $f(x) = \begin{cases} -x + 1 & -\pi \leq x \leq 0 \\ x + 1 & 0 \leq x \leq \pi \end{cases}$
10. Solve  $\left(\frac{x}{p}\right)^n + \left(\frac{y}{q}\right)^n = z^n$
11. Show that  $L\left(\frac{e^{at} - \cos bt}{t}\right) = \frac{1}{2} \log\left(\frac{s^2 + b^2}{(s - a)^2}\right)$ .
12. Determine the inverse laplace of  $\left(\frac{4s^2 - 3s + 5}{(s + 1)(s - 1)(s - 2)}\right)$ .
13. Verify Greens theorem for  $\oint_C (3x^2 - 8y^2)dx + (4y - 6xy)dy$ . Where C is the boundary of the region enclosed by the parabolas  $x^2 = y$  and  $y^2 = x$ .

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