SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai — 600 044. B.Sc.(Maths) END SEMESTER EXAMINATIONS APRIL-2023 SEMESTER - V 20UMACT5011 - Dynamics

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions $(6 \times 5 = 30 \text{ Marks})$

- 1. Find the magnitude and direction of the resultant of the velocities $\overline{v_1}$ and $\overline{v_2}$.
- 2. Show that, in a Simple harmonic motion, the sum of the Kinetic energy and Potential energy is a constant.
- 3. In a projectile, prove that $gT^2 = 2Rtan\alpha$, with usual notations.
- 4. State Laws of Impact.
- 5. State and prove perpendicular axis theorem.
- 6. If a point moves in a straight line with uniform acceleration and covers successive distances in times t_1, t_2, t_3 , then show that $\frac{1}{t_1} \frac{1}{t_2} + \frac{1}{t_3} = \frac{3}{t_1 + t_2 + t_3}$
- 7. A particle is moving with simple harmonic motion and while moving from the mean position to one extreme position , its distances at three consecutive seconds are x_1, x_2, x_3 . Show that its period is $\frac{2\pi}{\cos^{-1}((x_1 + x_3)/2x_2)}$.
- 8. Two equal balls of mass 'm' are in contact on a table. A third equal ball strikes both symmetrically and remains at rest after impact. Show that $e = \frac{2}{3}$.

Section C

Answer any **THREE** questions $(3 \times 10 = 30 \text{ Marks})$

- 9. Find the components of velocity and acceleration in radial and transverse direction.
- 10. Prove that the composition of two simple harmonic motion of same period is also simple harmonic with the same period.
- 11. Prove that the path of a projectile is a parabola.
- 12. Find the velocities of two smooth spheres after a direct impact between them.
- 13. Find the Moment of Inertia of a solid sphere.
