SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai — 600 044. B.Sc.(Statistics) - END SEMESTER EXAMINATIONS APRIL-2023

SEMESTER - I

20USTAT1001 - Allied Mathematics - I

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions $(6 \times 5 = 30 \text{ Marks})$ 1. Solve: $1 + \frac{3}{4} + \frac{3.5}{4.8} + \frac{3.5.7}{4.8.12} + \dots$ 2. Show that $\frac{e^2 + 1}{e^2 + 1} = \frac{\frac{1}{1!} + \frac{1}{3!} + \frac{1}{5!} + \dots}{1 + \frac{1}{2!} + \frac{1}{4!} + \dots}$

3. If $y = \frac{3}{(x+1)(2x-1)}$, Apply nth derivative to find y_n ,

4. If
$$x + y + z = u$$
, $y + z = v$ and $z = uvw$, show that $\frac{\partial(x, y, z)}{\partial(u, v, w)} = uv$

- 5. Show that $\frac{\sin 6\theta}{\sin \theta} = 32 \cos^5 \theta 32 \cos^3 \theta + 6 \cos \theta$
- 6. Apply $\cos \theta$ formula to express $\cos \theta$ in terms of $\cos \theta$.
- 7. Show that $U_n + n(n-1) U_{n-2} = n(\frac{\pi}{2})^n$ if $U_n = \int_0^{\pi/2} x^n sinxdx$ and n is a positive integer.
- 8. Examine for maximum or minimum value of $x^2 + y^2$ 4x-2y+10

Section C

Answer any **THREE** questions $(3 \times 10 = 30 \text{ Marks})$

- 9. Solve the series: $\frac{1}{2.3} + \frac{1}{4.5} + \frac{1}{6.7} + \dots$
- 10. If y = a cos (log x) + b sin (log x), Apply nth derivative to prove that $x^2y_{n+2} + (2n+1)xy_{n+1} (n^2+1)y_n = 0$
- 11. Examine the maximum and minimum of the function $2(x^2 y^2) x^4 + y^4$
- 12. Compute $\sin^8\theta$ and prove that $\sin^8\theta = \frac{1}{2^7} \left[\cos 8\theta - 8 \cos 6\theta + 28 \cos 4\theta - 56 \cos 2\theta + 35\right]$
- 13. Obtain the reduction formula for $\int sin^n x dx$