

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)
Chromepet, Chennai — 600 044.

B.Sc. - END SEMESTER EXAMINATIONS APRIL-2023
SEMESTER - II

16UCHAT2MA2 - Allied Mathematics - II

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions ($6 \times 5 = 30$ Marks)

- Find the Fourier Transform of $f(x)=x^2$ defined on $[-\pi, \pi]$
- Find $L[t^2 e^{3t} \sinh t]$
- Evaluate $L^{-1} \left[\log \frac{s+a}{s+b} \right]$
- Compute $\nabla \cdot \vec{F}$ and $\nabla \times \vec{F}$ at the Point (1,-1,1) for the function $\vec{F} = xz^3 \vec{i} - 2x^2yz \vec{j} + 2yz^4 \vec{k}$
- Solve : $zpq = p+q$.
- Find the Laplace transform of $e^{-t} \int_0^t t \cos t dt$.
- Find the Inverse Laplace transform of $\frac{1}{s(s+1)^2}$
- If $\vec{F} = xz \vec{i} + yz \vec{j} + z^2 \vec{k}$, then Evaluate $\int_C \vec{F} \cdot d\vec{r}$ from the point (0, 0, 0) to (1, 1, 1) where C is the curve given by $x = t$, $y = t^2$ and $z = t^3$.

Section C

Answer any **THREE** questions ($3 \times 10 = 30$ Marks)

- Find the Fourier Series of $f(x) = \begin{cases} x & 0 \leq x \leq \pi. \\ 2\pi - x & \pi \leq x \leq 2\pi \end{cases}$
- Solve: $(y-z)p + (z-x)q = x-y$
- Find the Laplace transforms of
 - $e^t \cos^3 t$
 - $\frac{\cosh at - \cosh bt}{t}$
- Evaluate $L^{-1} \left[\frac{5s+3}{(s-1)(s^2+2s+5)} \right]$
- Verify Green's Theorem for $\oint_C (3x^2 - 8y^2) dx + (4y - 6xy) dy$ Where C is the boundary of the region bounded by the parabolas $x^2 = y$ and $y^2 = x$.
