SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai — 600 044. M.Sc. - END SEMESTER EXAMINATIONS NOVEMBER - 2022 SEMESTER - III 20PAMCT3009 - Classical Mechanics

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

Section A

Answer any **SIX** questions $(6 \times 5 = 30 \text{ Marks})$

- 1. (i)Find the expression for kinetic energy of a system of particles.
 - (ii) State Conservation Theorem for the linear momentum of a particle.
- 2. State and prove D' Alembert's principle.
- 3. Prove that the shortest distance between two points in a plane is a straight line.
- 4. Compute the paths followed by a particle in sliding from one point to another in the absence of friction in the shortest time.
- 5. Obtain the derivation of Coriolis force.
- 6. Define scalar dot product and double dot product of dyads.
- 7. Derive the Hamilton's equation from Lagrange's equation by means of Legendre transformation.
- 8. Define Poisson bracket and prove that the Poisson bracket is invariant with respect to a canonical transformation.

Section B

Part A

Answer any **TWO** questions $(2 \times 10 = 20 \text{ Marks})$

- 9. (i)Show that if the forces acting on a particle are conservative, then the total energy of the particle is conserved.
 - (ii) Derive Lagrange's equation of motion for Atwood's machine
- 10. Derive Euler Lagrangian differential equation.
- 11. Prove that the real orthogonal matrix specifying the physical motion of a rigid body with one point fixed always has the eigen value +1.
- 12. Compute the equation of moment of inertia about the axis of rotation.

Part B

Compulsory question $(1 \times 10 = 10 \text{ Marks})$

13. Solve the problem of simple harmonic oscillator in one dimension by considering the Hamiltonian equation $H=\frac{(p^2+m^2\omega^2q^2)}{2m}$ using canonical transformation.

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