

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)
Chromepet, Chennai — 600 044.

B.C.A. - END SEMESTER EXAMINATIONS NOVEMBER-2022
SEMESTER - I

20UCAAT1001 - Allied Mathematics-I

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

Section A

Answer any **SIX** questions ($6 \times 5 = 30$ Marks)

1. Define Discrete Mathematics and explain about disadvantages of discrete Mathematics.
2. Express $\frac{\sin 7\theta}{\sin \theta}$ as a polynomial in $\sin \theta$.
3. Prove that $\cosh^{-1}x = \pm \log(x + \sqrt{x^2 - 1})$
4. Evaluate $L(e^{-3t} \sin t \cos t)$.
5. Find the inverse transform of the following
(i) $\frac{1}{s-7}$ (ii) $\frac{1}{s+3}$ (iii) $\frac{1}{s^2+4}$ (iv) $\frac{1}{s^5}$
6. Show that $2^5 \cos^6 \theta = \cos 6\theta + 6\cos 4\theta + 15\cos 2\theta + 10$.
7. Evaluate $L(\sin 3t \cos 2t)$ and $L(\cos 2t \cos t)$.
8. Find the inverse transform of the following $\frac{1}{s^2(s+4)}$.

Section B

Answer any **THREE** questions ($3 \times 10 = 30$ Marks)

9. Explain the basic logical operation.
10. Show that $\cos 8\theta = 128 \cos^8 \theta - 256 \cos^6 \theta + 160 \cos^4 \theta - 32 \cos^2 \theta + 1$.
11. If $\cos(A + iB) = x + iy$, then show that
$$\frac{x^2}{\cos^2 A} - \frac{y^2}{\sin^2 A} = 1 \text{ and } \frac{x^2}{\cosh^2 B} + \frac{y^2}{\sinh^2 B} = 1.$$
12. Find the Laplace Transform of the following
(i) $\sin 2t \sin t$ (ii) $\cos 4t \cos 2t$ (iii) $3 \cosh 2t$.
13. Find the inverse Laplace transform of $\frac{4s^2 - 3s + 5}{(s+1)(s-1)(s-2)}$.
