21UCGAT1001

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai — 600 044. B.Sc. END SEMESTER EXAMINATIONS NOVEMBER-2022 SEMESTER - I 21UCGAT1001 - Discrete Mathematics

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

Section A

Answer any **SIX** questions $(6 \times 5 = 30 \text{ Marks})$

1. Define Conjunction and Disjunction with truth tables.

2. Show that (i) $]] P \iff P$ (ii) $(P \rightarrow Q) \lor (Q \rightarrow P)$

- 3. Prove that the Composition of functions is associative.
- 4. Let A={1,2,3} and B={1,4} and consider the relation R such that "<" then find R, R^c and R⁻¹.
- 5. (i) Define Group.
 - (ii) Check whether $(Z_5, +5)$ is an abelian group of order 5.
- 6. Examine whether the following pairs of graphs G_1 , G_2 given below are isomorphic or not.





- 7. State the properties of Hamiltonian Graph.
- 8. Find the minimum spanning tree for the following graph.



Section B

Answer any **THREE** questions $(3 \times 10 = 30 \text{ Marks})$

- 9. (i) Define Tautology with truth table
 - (ii) Construct the truth table for $P \lor (Q \land R) \iff (P \lor Q) \land (P \lor R)$
- 10. Using Characteristic functions, prove that $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$
- 11. State and prove cancellation laws of group.
- 12. Prove that a connected graph G is Eulerian iff all the vertices are of even degree.
- 13. Explain Dijkstra's Algorithm for shortest path with example.
