

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)

Chromepet, Chennai — 600 044.

B.Sc.(AI) - END SEMESTER EXAMINATIONS APRIL-2023

SEMESTER - I

22UAIAT1001 - Allied Mathematics - I

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions ($6 \times 5 = 30$ Marks)

1. Using Newton forward formula, find $f(43)$

x	40	50	60	70	80	90
f(x)	184	204	226	250	276	304

2. Prove that $S = \Delta(1 + \Delta)^{-1/2} = \nabla(1 - \nabla)^{-1/2}$

3. Find eigen value and eigen vector of the Matrix $\begin{bmatrix} 4 & 1 \\ 3 & 2 \end{bmatrix}$.

4. Expand $\sin 5\theta$ in power of $\sin \theta$ and $\cos \theta$.

5. If $Y = \frac{\log x}{y}$, find second derivatives.

6. Find the Equation whose roots are given $3 + \sqrt{5}$.

7. If $X = u(1+v)$ and $Y = v(1+u)$, find $\frac{\partial(x, y)}{\partial(u, v)}$.

8. If $y = x^2 e^x$, prove that $y_n = \frac{1}{2}n(n-1) y_2 - n(n-2)y_1 + (n-1)(n-2)y$ using Leibnitz's theorem.

Section C

Answer any **THREE** questions ($3 \times 10 = 30$ Marks)

9. Find the value of $F(3.5)$ using the following table

X	3	4	5	7
F(X)	31	69	131	351

10. Find the eigen Value and eigen Vector of $A = \begin{bmatrix} 3 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 3 \end{bmatrix}$

11. Solve: $6x^4 - 25x^3 + 37x^2 - 25x + 6$.

12. Expand $\sin^5 \theta \cdot \cos^4 \theta$.

13. Find the extreme value of $f(x, y) = xy - x^2 - y^2 - 2x - 2y + 4$.
