

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)
Chromepet, Chennai — 600 044.

B.Sc.(Chemistry) END SEMESTER EXAMINATIONS NOVEMBER -2023

SEMESTER - II

20UCHAT2002 - Allied Mathematics - II

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions ($6 \times 5 = 30$ Marks)

1. Define Fourier Series in the interval $(0, 2\pi)$, and also write the Dirichlets condition in Fourier Series.
2. Find Fourier Series for the function $f(x) = x^2$ defined in the interval $(-\pi, \pi)$.
3. Solve $z = px + qy + \sqrt{1 + p^2 + q^2}$.
4. Form partial differential equation by eliminate the arbitrary function from $z = f(x^2 + y^2)$.
5. Define Laplace transform with an example and write any two properties of Laplace transform.
6. Predict the value of $L(\sin^2(2t))$.
7. Calculate $L^{-1}\left[\frac{1}{(s+2)^2 + 16}\right]$
8. Find the directional derivative of $\phi(x, y, z) = x y^2 + y z^3$.

Section C

Answer any **THREE** questions ($3 \times 10 = 30$ Marks)

9. Express $f(x) = \frac{1}{2}(\pi - x)$ as Fourier series with period 2π , to be valid in the interval 0 to 2π .
10. Determine the general solution of $(y+z)p + (z+x)q = x+y$.
11. Evaluate $L(t e^{-t} \sin t)$.
12. Evaluate $L^{-1}\left[\frac{1}{s(s+1)(s+2)}\right]$
13. Prove that $F = (y^2 \cos x + z^3)i + (2y \sin x - 4)j + (3x z^2 + 2)k$ is irrotational and find its scalar potential.
