SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai — 600 044. B.Sc.(Computer Science) END SEMESTER EXAMINATIONS NOVEMBER -2023 SEMESTER - II 20UCSAT2002 - Allied Mathematics - II

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions $(6 \times 5 = 30 \text{ Marks})$

- 1. Find the positive root of $x^3 x = 1$ correct to 2 decimal places by bisection method
- 2. Find the 7^{th} term of the sequence 2,9,28,65, 126, 217 and also find the general term.
- 3. Using Lagrange's Interpolation formula, find , from the following table.

х	5	6	9	11
у	12	13	14	16

4. The population of a certain city is given below. Find $\frac{dy}{dx}$ at x = 1931

Year	Х	1931	1941	1951	1961	1971
Population in thousands	У	40.62	60.80	79.95	103.56	132.65

- 5. Using Taylor series method find, correct to 3 decimal places, the value of y(0.1) given $y^\prime=x^2+y^2$ and y(0)=1
- 6. Using Newton Raphson method, find the root between 0 and 1 of $x^3 = 6x 4$ correct to 5 decimal places
- 7. Compute y at x = 0.4 by Euler method given y' = xy, y(0) = 1

8. Show that
$$riangle_{bcd}^3\left(\frac{1}{a}\right) = -\frac{1}{abcd}$$

Section C

Answer any **THREE** questions $(3 \times 10 = 30 \text{ Marks})$

9. Solve for positive root of $x^3 - 4x + 1 = 0$ by Regula Falsi method

10. Find the value of y at x = 21 and x = 28, from the following data

x	20	23	26	29
у	0.3420	0.3907	0.4384	0.4848

Contd...

11. Using Newton's Divided difference formula, find the value of f(2), f(8) and f(15) from the table given below:

X		4	5	7	10	11	13
	x)	48	100	294	900	1210	2028

- 12. Evaluate $I = \int_{0}^{6} \frac{1}{1+x} dx$ using
 - i. Trapezoidal rule
 - ii. Simpson's $\frac{1}{3}$ rule iii. Simpson's $\frac{3}{8}$ rule
 - Also, checkup by direct integration
- 13. Apply the fourth order Runge-Kulta method to find y(0.2) given that $y^\prime=x+y, y(0)=1$
