SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)

Chromepet, Chennai — 600 044. B.Sc.(Physics) END SEMESTER EXAMINATIONS NOVEMBER -2023

SEMESTER - III

22UPHCT3005 - Mathematical Physics and Statistical Mechanics

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions
$$(6 \times 5 = 30 \text{ Marks})$$

1. Find the eigen values of the matrix, A = $\begin{pmatrix} 6 & -6 & 5 \\ 14 & -13 & 10 \\ 7 & -6 & 4 \end{pmatrix}$

2. Checks whether the matrix $\begin{pmatrix} 1/\sqrt{2} & i/\sqrt{2} \\ -i/\sqrt{2} & -1/\sqrt{2} \end{pmatrix}$ is unitary.

- 3. Arrive at the relation between beta and gamma functions.
- 4. Evaluate $\int_{0}^{\infty} \frac{x^{8}(1-x^{6})}{(1+x)^{24}} dx$
- 5. Evaluate $J_{\frac{1}{2}}(x)$
- 6. Write brief notes on microstates and macrostates with suitable examples.
- 7. State the postulates of classical statistics.
- 8. Compare B-E, F-D and M-B statistics.

Section C

Answer any **THREE** questions $(3 \times 10 = 30 \text{ Marks})$

9. Verify Cayley - Hamilton theorem and hence find the inverse for $\begin{pmatrix} 1 & 3 & 7 \\ 4 & 2 & 3 \\ 1 & 2 & 1 \end{pmatrix}$

10. Evaluate:

(i)
$$\int_0^1 \frac{dx}{\sqrt{1-x^n}}$$

(ii) $\int_0^1 \frac{dx}{(1-x^n)^{1/n}}$

- 11. Arrive at the equation for Laguerre polynomial from the Laguerre's differential equation.
- 12. Arrive at an equation for Maxwell Boltzmann distribution law.
- 13. Derive the equation of Bose Einstein distribution law.

22UPHCT3005

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