SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai — 600 044. B.Sc.(Statistics) END SEMESTER EXAMINATIONS NOVEMBER -2023 SEMESTER - I

## 20USTAT1001 - Allied Mathematics - I

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

## Section B

Answer any **SIX** questions  $(6 \times 5 = 30 \text{ Marks})$ 1. Show that  $\frac{1}{1!} + \frac{1+2}{2!} + \frac{1+2+3}{3!} + ... = \frac{3e}{2}$ 2. Show that  $\frac{1}{12} + \frac{1}{34} + \frac{1}{56} + ... = log2$ . 3. Find the nth derivative of  $e^{ax}$  with respect to x. 4. Find the nth derivative of  $y = \frac{1}{r^2 + 5r + 6}$ . 5. If  $x = rcos\theta$ ,  $y = rsin\theta$ , then find  $\frac{\partial(x,y)}{\partial(r,\theta)}$ . 6. Show that  $2^6 \cos^7 \theta = \cos 7\theta + 7\cos 5\theta + 21\cos 3\theta + 35\cos \theta$ . 7. If  $\frac{\sin \theta}{\theta} = \frac{2165}{2166}$ . show that  $\theta$  is equal to 3° 1' nearly. 8. Evaluate  $\int_{1}^{\pi/2} \cos^9 x dx$ .

## Section C

Answer any **THREE** questions  $(3 \times 10 = 30 \text{ Marks})$ 

9. Show that 
$$\sqrt{8} = 1 + \frac{3}{4} + \frac{3.5}{2.4^2} + \frac{3.5.7}{2.3.4^3} + \dots$$

10. If  $y = \sin^{-1} x$ , prove that

i)  $(1 - x^2)y_2 - xy_1 = 0$ . ii)  $(1 - x^2)y_{n+2} - (2n + 1)xy_{n+1} - n^2y_n = 0.$ 

## 11. Find maximum and minimum values of the function $f = x^2y^2$ - $x^2$ - $y^2$ .

- 12. Express  $\frac{\sin 5\theta}{\sin \theta}$  as a polynomial in  $\cos \theta$ .
- 13. Obtain the reduction formula for  $\int sin^n x \, dx$ .