SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai — 600 044. M.Sc.(Bio-Statistics) END SEMESTER EXAMINATIONS NOVEMBER - 2023 SEMESTER - I **20PBSCT1002 - Statistical Inference - I** 

Total Duration : 2 Hrs. 30 Mins.

Total Marks : 60

## Section B

Answer any **SIX** questions  $(6 \times 5 = 30 \text{ Marks})$ 

- 1. Define unbiasedness and consistency of an estimator with suitable example.
- 2. Explain censored data.
- 3. Compute confidence interval for mean of  $N(\mu, \sigma^2), \sigma$  known.
- 4. Explain prior distribution and conjugate prior distribution.
- 5. State and Prove Rao-Blackwell Theorem.
- 6. Compute maximum likelihood estimator of P when  $X_1, X_2, ..., X_n \sim b(n, p)$
- 7. Describe interval estimation.
- 8. Distinguish between Baye's interval estimation and interval estimation.

## Section C

I - Answer any **TWO** questions  $(2 \times 10 = 20 \text{ Marks})$ 

- 9. State and Prove Cramer Rao lower bound.
- 10. State and Prove Lehmann-Scheffe Theorem.
- 11. Explain the method of minimum chi square.
- 12. Compute 100 (1- $\alpha$ )% confidence interval for the parameter  $\theta$  of the distribution  $dF(x) = \theta e^{-\theta x} 0 < x < \infty$

II - Compulsory question  $(1 \times 10 = 10 \text{ Marks})$ 

13. Let  $X \sim b(n, p)$  and  $L(p, \delta(x)) = \{p-\delta(x)\}^2$ . Let be the prior pdf of p. Compute Baye's estimator

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