

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)
Chromepet, Chennai — 600 044.

BCA END SEMESTER EXAMINATIONS NOVEMBER -2023

SEMESTER - I

20UCAAT1001 - Allied Mathematics - I

Total Duration : 2 Hrs 30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions ($6 \times 5 = 30$ Marks)

1. Show that $(p \wedge q) \wedge \sim (p \vee q)$ is a Tautogy or contradiction.
2. Expand $\sin^7 \theta$ in a series of sines of multiples of θ .
3. Express $\frac{\sin 6\theta}{\sin \theta}$ in terms of $\cos \theta$.
4. If $\cos(x + iy) = \cos \theta + i \sin \theta$ then prove that $\cos 2x + \cosh 2y = 2$.
5. Find i) $L(e^{-at} \sin 6t)$ ii) $L[t \sin 2^t]$.
6. Prove that $L(t^n) = \frac{n!}{s^{n+1}}$ if n is a positive integer.
7. Find $L^{-1} \left(\frac{1}{s(s+1)(s+2)} \right)$
8. Find $L^{-1} \left(\frac{s-3}{s^2+4s+13} \right)$

Section C

Answer any **THREE** questions ($3 \times 10 = 30$ Marks)

9. Construct the Truth Table for the following and write the Truth Set for the following $p \Rightarrow [(p \vee r) \wedge \sim (p \Leftrightarrow \sim r)]$
10. Expand $\cos^6 \theta$ and $\cos^5 \theta$ in series of cosines of multiples of θ .
11. If $\cos \alpha \cos \beta = \cos \phi$; $\sin \alpha \sin \beta = \sin \phi$ then prove that $\sin \phi = \pm \sin^2 \alpha = \pm \sin^2 \beta$.
12. (i) find the Laplace transform of $(\sin at - at \cos at)$.
(ii) Find $L(\sin^3 2t)$
13. Find the inverse Laplace Transform of $\frac{1}{3-4s} + \frac{3-2s}{s^2+49}$
