SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai - 600 044. BSc. Chemistry - END SEMESTER EXAMINATIONS APRIL - 2024 SEMESTER - II 20UCHAT2002 - Allied Mathematics II

Total Duration : 2 Hrs. 30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions $(6 \times 5 = 30 \text{ Marks})$

- 1. Express $f(x) = (\pi x)^2$ as a Fourier series of periodicity 2π in $0 < x < 2\pi$.
- 2. Eliminate the arbitrary constant a and b from $z = (x^2 + a^2) (y^2 + b^2)$.
- 3. Form the partial differential equation from $z = f(x^2 + y^2 + z^2)$.
- 4. Solve $p^2 + q^2 = m^2$.
- 5. Solve (mz ny) p + (nx lz) q = ly mx.
- 6. Find the Laplace transform of $t^3 + e^{3t}$.
- 7. State and prove linear property of Laplace transform.
- 8. Find the Laplace transform of te^{2t} .

Section C

Answer any **THREE** questions $(3 \times 10 = 30 \text{ Marks})$

- 9. Expand $f(x) = x x^2$ as a Fourier series in $(-\pi, \pi)$.
- 10. Form the partial differential equation from
 - (i) z = ax + by + a/b.

(ii)
$$f(x + y + z, xy + z^2) = 0$$
.

11. Solve (i)
$$x(y - z) p + y(z - x)q = z(x - y)$$
. (ii) $p(1 + q) = qz$.

- 12. Find the Laplace transform of
 (i) (t + 1)²
 (ii) Cos²t
 (iii) Sin(at + b)
- 13. (a) State and prove first shifting theorem.
 (b) Find the Laplace transform of (i) t²e^{-4t} (ii) (1 e^{-t}) / t.

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