SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai - 600 044. B.Sc. Maths - END SEMESTER EXAMINATIONS APRIL - 2024 SEMESTER - VI 20UMAET6002 - Formal Languages and Automata Theory

Total Duration : 2 Hrs. 30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions $(6 \times 5 = 30 \text{ Marks})$

- 1. Explain types of grammars with example.
- 2. Construct a Regular grammar to generate the language $L = \{a^n b^m / n, m \ge 1\}$
- 3. Show that the family of CFL is closed under union.
- 4. Prove that the family of regular languages are closed under reflection.
- 5. State and prove Chomsky Normal form theorem.
- 6. Construct an ambiguous and unambiguous grammar for the language $\{a^nb^n/n=1\}$
- 7. Reduce the grammar to CNF $S \rightarrow aAD, A \rightarrow aB / bAB, B \rightarrow b, D \rightarrow d$
- 8. Construct an finite automaton that accepts the language L(M), the set of strings with even number of 0's and 1's.

Section C

Answer any **THREE** questions $(3 \times 10 = 30 \text{ Marks})$

- 9. Construct a grammar to generate the context sensitive language $L = \{a^n b^m a^n b^m / n, m = 1\}$
- 10. Define star of L and show that the family of PSL, CSL, CFL and RL are closed under star.
- 11. Prove that for any context free grammar G there exists an equivalent context free grammar G_1 such that for each non-terminal $A \neq S$ in G_1

 $L_A = \{ w | A \Longrightarrow w, w \in T^* \}$ is infinite.

Contd...

12. Compute the finite Automaton of the following transition diagram. Also mention the output of the string 01001.



13. Let L be set accepted by a nondeterministic finite automaton. Then prove that there exists a deterministic finite automaton that accepts L.
