20UMAAT4004

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai - 600 044. B.Sc. Maths - END SEMESTER EXAMINATIONS APRIL - 2024 SEMESTER - IV 20UMAAT4004 - Mathematical Statistics II

Total Duration : 2 Hrs. 30 Mins.

Total Marks : 60

## Section B

Answer any **SIX** questions  $(6 \times 5 = 30 \text{ Marks})$ 

- 1. Derive student's t-distribution.
- 2. State and prove the additive property of Chi-square distribution.
- 3. Define estimator and what are the characteristics of estimators?
- 4. What are the properties of maximum likelihood estimators?
- 5. Define the following:
  - a) Null and Alternative hypothesis
  - b) Type I and Type II errors.
- 6. Write a note on critical region and Level of significance.
- 7. Write a note on Goodness of fit tests based on Chi-square.
- 8. Explain Test of independence of attributes on contingency table.

## Section C

Answer any **THREE** questions  $(3 \times 10 = 30 \text{ Marks})$ 

- 9. Define F-distribution and derive its PDF.
- 10. State and prove Cramer-Rao inequality.
- 11. Derive confidence Interval for the variance of two independent normal distribution with unknown means.
- 12. Explain test of significance for difference of proportions.

13. For the 2x2 table 
$$\begin{vmatrix} \mathbf{a} & \mathbf{b} \\ \mathbf{c} & \mathbf{d} \end{vmatrix}$$
 Prove that Chi-square test of independence gives  

$$\chi^2 = \frac{N(ad - bc)^2}{(a+c)(b+d)(a+b)(c+d)}, \mathbf{N} = \mathbf{a} + \mathbf{b} + \mathbf{c} + \mathbf{d}.$$

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