

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)
Chromepet, Chennai - 600 044.

B.Sc. Physics - END SEMESTER EXAMINATIONS APRIL - 2024

SEMESTER - IV

20UPHAT4004 - Allied Mathematics II

Total Duration : 2 Hrs. 30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions ($6 \times 5 = 30$ Marks)

- Find the Fourier series for the function $f(x) = e^x$ in $(-\pi, \pi)$.
- Form a partial differential equation by eliminating the constants 'a' and 'b' from The equation $z = (x+a)(y+b)$.
- Solve $\frac{\partial^2 z}{\partial x^2} = \sin x$.
- Solve $xp + p^2 = q$.
- Solve the equation $p^2 + q^2 = x + y$.
- Find $L(e^t + \frac{1}{e^t})^2$.
- Evaluate $L(e^{-3t} \sin t \cos t)$.
- If $f(t) = e^{-2t} \sin 2t$, find $L[f'(t)]$.

Section C

Answer any **THREE** questions ($3 \times 10 = 30$ Marks)

- Find the Fourier series for $f(x)$ in $-\pi < x < \pi$ if

$$f(x) = \begin{cases} -a, & -\pi < x < 0 \\ a, & 0 < x < \pi \end{cases}.$$
- Eliminate the arbitrary functions f_1 and f_2 from the equation $z = f_1(x+y) + f_2(x-y)$.
- Solve the equation $xp + zq = y$.
- Find the Laplace transforms of (i) $\cos(at+b)$ (ii) $\sin(2t+3)$.
- Show that
 - $L(\cos at - \frac{1}{2}at \sin at) = \frac{S^3}{(S^2+a^2)^2}$.
 - $[\frac{1}{2}(\sin at - at \cos at)] = \frac{a^3}{(S^2+a^2)^2}$.
