

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN  
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)  
Chromepet, Chennai - 600 044.

B.Sc. Statistics - END SEMESTER EXAMINATIONS APRIL - 2024

SEMESTER - IV

**20USTCT4007 - Statistical Inference - I**

Total Duration : 2 Hrs. 30 Mins.

Total Marks : 60

### Section B

Answer any **SIX** questions ( $6 \times 5 = 30$  Marks)

1. State and prove Invariance properties of consistent estimator.
2. Explain the method of moments.
3. Discuss the confidence Interval for proportion with example.
4. Describe the F-test for equality of variances of two populations.
5. State and prove Rao- Blackwell theorem.
6. Find the maximum likelihood estimate of the parameter  $\theta$  of the distribution.  
$$f(x : \theta) = \frac{1}{2}e^{-|x-\theta|}$$
7. Prepare a note on assumptions about  $t$ -test.
8. Infer the chi square test for goodness of fit.

### Section C

Answer any **THREE** questions ( $3 \times 10 = 30$  Marks)

9. Describe
  - a. State Neyman Pearson factorization theorem.
  - b. Give the Properties of Estimators.
  - c. Explain in detail about Consistency and sufficiency of statistic.
10. State and prove Cramer-Rao inequality.
11. A random sample of size  $n$  is drawn from a normal population  $N(\mu, \sigma^2)$ . Estimate  $\mu$  and  $\sigma^2$  by the method of maximum likelihood.
12. Derive the  $100(1-\alpha)\%$  confidence interval for the variance ratio of two independent normal distributions with unknown means.
13. (i) Prove MVUBE is Unique.  
(ii) State and prove sufficiency Condition for consistent estimator.

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