SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai - 600 044. M.Sc. Appl.Maths - END SEMESTER EXAMINATIONS APRIL - 2024 SEMESTER - IV 20PAMCT4011 - Differential Geometry and Tensor Calculus

Total Duration : 2 Hrs. 30 Mins.

Total Marks : 60

## Section B

Answer any **SIX** questions  $(6 \times 5 = 30 \text{ Marks})$ 

- 1. Give the equation of a circular helix and find the length of one complete turn.
- 2. Describe the Osculating sphere giving its centre of spherical curvature and radius of spherical curvature.
- 3. Explain how the anchor ring is generated and give the equation of the surface of revolution.
- 4. How is the Helicoid generated. Differentiate between the right helicoid and the general helicoid.
- 5. Find the orthogonal trajectories of the sections by the planes z = constant on the paraboloid  $x^2 y^2 = z$ .
- 6. A particle is constrained to move on a smooth surface under no force except the normal reaction. Prove that its path is a geodesic.
- 7. Show that the sum of two tensors which have the same number of covariant and the same number of contravariant indices is again a tensor of the same type and rank as the given tensors.
- 8. Prove the quotient law of tensors.

## Section C

I - Answer any **TWO** questions  $(2 \times 10 = 20 \text{ Marks})$ 

- 9. Obtain the curvature and torsion of the curve of intersection of the 2 quadratic surfaces  $ax^2 + by^2 + cz^2 = 1$ ,  $a'x^2 + b'y^2 + c'z^2 = 1$ .
- 10. State and prove the Fundamental existence theorem for space curves.
- 11. A helicoid is generated by the screw motion of a straight line skew to the axis. Find the curve coplanar with the axis which generates the same helicoid.

12. If a transformation of coordinates T possesses an inverse T<sup>-1</sup> and if J and K are the Jacobians of T and T<sup>-1</sup> respectively then JK = 1.Validate this statement.

II - Compulsory question  $(1 \times 10 = 10 \text{ Marks})$ 

13. Prove that the curves of the family  $v2/u^2 = c$  are geodesics on a surface with metric  $v^2 du^2 - 2uv du dv + 2u^2 dv^2 (u > 0, v > 0)$ .

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