

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)
Chromepet, Chennai - 600 044.

M.Sc. Appl Maths - END SEMESTER EXAMINATIONS APRIL - 2024

SEMESTER - II

20PAMET2002 - Mathematical Statistics

Total Duration : 2 Hrs. 30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions ($6 \times 5 = 30$ Marks)

1. If T_n is a sequence of estimators such that $ET_n \rightarrow \psi(\theta)$ and $\text{var}(T_n) \rightarrow 0$ as $n \rightarrow \infty$, then prove that T_n is consistent for $\psi(\theta)$.
2. Let $X \sim b(1, \theta^2)$. Does there exist an unbiased estimator of θ ?
3. Find confidence interval for mean of normal population when the variance is known.
4. Let X_1, X_2, \dots, X_n be a sample from $N(\mu, \sigma^2)$. Find the method of Moments estimator for the parameters (μ, σ^2) .
5. Let X be an RV with PMF under H_0 and H_1 given by

x	1	2	3	4	5	6
$f_0(x)$	0.01	0.01	0.01	0.01	0.01	0.95
$f_1(x)$	0.05	0.04	0.03	0.02	0.01	0.85

Find $\lambda(x)$

6. The standard deviation of capacity for batteries of a standard type is known to be 1.66 ampere-hours. The following capacities (ampere-hours) were recorded for 10 batteries of a new type: 146, 141, 135, 142, 140, 143, 138, 137, 142, 136. Does the new battery differ from the standard type with respect to variability of capacity?
7. The mean life of a sample of 9 light bulbs was observed to be 1309 hours with a standard deviation of 420 hours. A second sample of 16 bulbs chosen from a different batch showed a mean life of 1205 hours with a standard deviation of 390 hours. Test whether there is a significant difference between the means of the two batches, assuming that the population variances are the same

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8. Describe the layout and the model for two way analysis of variance with one observation per cell.

Section C

I - Answer any **TWO** questions ($2 \times 10 = 20$ Marks)

9. Find the CRK bound for the variance of an unbiased estimator of θ in sampling from $N(\theta, 1)$
10. A die is rolled 120 times with the following results:

Result :	1	2	3	4	5	6
Frequency:	20	0	20	25	15	10

Test the hypothesis that the die is fair at 95%

11. If a sufficient statistic T exists for the family $\{f_{\theta} = \in \Theta\}$, $\Theta = \{\theta_0, \theta_1\}$, then prove that Neyman-Pearson MP test is a function of T .
12. A manufacturer claims that the lifetime of a certain brand of batteries produced by his factory has a variance of $5000 (\text{hours})^2$. A sample of size 26 has a variance of $7200 (\text{hours})^2$. Assuming that it is reasonable to treat these data as a random sample from a normal population, test the manufacturer's claim at the 98% level of significance.

II - Compulsory question ($1 \times 10 = 10$ Marks)

13. The following are the coded values of the amounts of corn (in bushels per acre) obtained from four varieties, using unequal number of plots for the different varieties:

A: 2, 1, 3, 2

B: 3, 4, 2, 3, 4, 2

C: 6, 4, 8

D: 7, 6, 7, 4

Test whether there is a significant difference between the yields of the varieties.
