

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN  
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)  
Chromepet, Chennai - 600 044.

B.Sc.Mathematics - END SEMESTER EXAMINATIONS - NOV'2024

SEMESTER - III

**20UMACT3005 - Differential Equations and Laplace Transforms**

Total Duration : 2 Hrs.30 Mins.

Total Marks : 60

### Section B

Answer any **SIX** questions ( $6 \times 5 = 30$  Marks)

1. Solve  $x^2p^2 + 3xyp + 2y^2 = 0$ .
2. Illustrate  $y = (x - a)p - p^2$ .
3. Solve  $(D^2 - 4D + 3)y = e^{-x} \sin x$ .
4. Interpret the result  
 $yz(ax + y + z)dx + zx(x + ay + z)dy + xy(x + y + az)dz = 0$ .
5. Compute  $q = xp + p^2$ .
6. Solve  $(y + z)p + (z + x)q = x + y$ .
7. Evaluate  $L(\sin^3 2t)$ .
8. Find  $L^{-1} \frac{s + 2}{(s^2 + 4s + 5)^5}$ .

### Section C

Answer any **THREE** questions ( $3 \times 10 = 30$  Marks)

9. Solve  $x^2 = (1 + p^2)$ .
10. Classify  $(D^2 + 16)y = 2e^{-3x} + \cos 4x$ .
11. Examine  $p^2 + q^2 = npq$ .
12. Evaluate  $\int_0^\infty \frac{e^{-t} - e^{-2t}}{t} dt$ .
13. Discriminate that the solution of the differential equation  $\frac{d^2y}{dt^2} + 4y = A$  is such that  $y = 0$  and  $\frac{dy}{dt} = 0$ , when  $t = 0$ .

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