SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN (AUTONOMOUS) (Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC) Chromepet, Chennai - 600 044. B.Sc.Statistics - END SEMESTER EXAMINATIONS - NOV'2024 SEMESTER - II 20USTCT2004 - Matrix Algebra

Total Duration : 2 Hrs.30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions $(6 \times 5 = 30 \text{ Marks})$

- 1. Explain the various types of matrices.
- 2. Define matrix multiplication and illustrate with an example. State two properties of matrix multiplication.
- 3. Explain how to convert a given matrix to its echelon form. Provide an example.
- 4. State and prove any two properties of determinants.
- 5. Show that every homogeneous system of linear equations has at least one solution.
- 6. State the properties of the characteristic polynomial of a matrix.
- 7. List out the Properties of Eigenvalues.
- 8. Explain various types of Quadratic Forms.

Section C

Answer any **THREE** questions $(3 \times 10 = 30 \text{ Marks})$

- 9. Show that for any orthogonal matrix Q, the inverse is equal to its transpose, $Q^{-1}=QT$. Provide an example.
- 10. State and prove Cayley Hamilton theorem.
- 11. Describe Cramer's rule for finding solution of system of linear equations.
- 12. Explain form and its properties of(i) Canonical method (ii) Echelon method
- 13. Prove that the index of a quadratic form is equal to the number of positive eigenvalues of the corresponding matrix. Use an example to illustrate your proof.
