

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN  
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)

Chromepet, Chennai - 600 044.

B.Sc.DS - END SEMESTER EXAMINATIONS - NOV'2024

SEMESTER - IV

**22UDSAT4004 - Allied Statistics - II**

Total Duration : 2 Hrs.30 Mins.

Total Marks : 60

### Section B

Answer any **SIX** questions ( $6 \times 5 = 30$  Marks)

1. Explain the following with examples.
  - (i) Exhaustive event
  - (ii) Mutually exclusive event
  - (iii) Equally likely event
  - (iv) Independent event
2. Derive mean and variance of Binomial distribution.
3. A continuous random variable has the pdf

$$f(x) = \begin{cases} 6x(1-x) & 0 \leq x \leq 1 \\ 0 & \text{Otherwise} \end{cases}$$

Determine the number b such that  $P(X < b) = P(X > b)$

4. Derive the MLE of parameter  $\lambda$  of the poisson distribution.
5. Certain refined edible oil is packed in tins holding 16 kg each. The filling machine can maintain this but with a standard deviation of 0.5 kg. samples 25 are taken from the production line. If a sample mean is 16.35 kg. can we be 95% sure that the sample has come from a population of 16 kg tins?
6. State and prove multiplication theorem.
7. Explain briefly about the properties of Normal distribution.
8. Derive Maximum likelihood estimate of Binomial distribution.

### Section C

Answer any **THREE** questions ( $3 \times 10 = 30$  Marks)

9. Define Axiomatic approach of probability also state and prove addition theorem.
10. Derive mean and variance of Poisson distribution.

**Contd...**

11. A continuous random variable  $x$  has the following pdf  $f(x) = \begin{cases} 3x^2 & \text{for } 0 < x < 1 \\ 0 & \text{Otherwise} \end{cases}$

Verify that it is a pdf and evaluate the following probabilities.

(i)  $P\left(X \leq \frac{1}{3}\right)$    (ii)  $P\left(\frac{1}{3} \leq X \leq \frac{1}{2}\right)$    (iii)  $P\left(X \leq \frac{1}{2} / \frac{1}{3} \leq X \leq \frac{2}{3}\right)$

12. obtain the MLE of  $\mu$  and  $\sigma^2$  of normal distribution  $N(\mu, \sigma^2)$ .

13. The following figures relate to production in kgs. of three variables A, B, C of wheat sown on 12 plots.

<b>A</b>	14	16	18		
<b>B</b>	14	13	15	22	
<b>C</b>	18	16	19	19	20

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