

SHRIMATHI DEVKUNVAR NANALAL BHATT VAISHNAV COLLEGE FOR WOMEN
(AUTONOMOUS)

(Affiliated to the University of Madras and Re-accredited with 'A+' Grade by NAAC)

Chromepet, Chennai - 600 044.

B.Sc.AI - END SEMESTER EXAMINATIONS - NOV'2024

SEMESTER - II

22UAIAT2002 - Allied Mathematics - II

Total Duration : 2 Hrs.30 Mins.

Total Marks : 60

Section B

Answer any **SIX** questions ($6 \times 5 = 30$ Marks)

1. Evaluate $\int x^4 \cos x dx$.
2. Find the Fourier series for $\sin^3 x$ in $[0, 2\pi]$.
3. Find the Fourier series for $f(x)$ in $(-\pi, \pi)$ if

$$f(x) = 0 \quad -\pi < x < 0,$$

$$f(x) = \pi \quad 0 < x < \pi$$
4. Solve $(D^2 + 5D + 4)y = 0$.
5. Solve $(D^2 - 4D + 13)y = e^{2x} \cos 3x$.
6. Eliminate the arbitrary function f from $f(xy + z^2, x + y + z) = 0$.
7. Solve $pq + p + q = 0$.
8. Find the Laplace transform of $L(t^2 \cos at)$.

Section C

Answer any **THREE** questions ($3 \times 10 = 30$ Marks)

9. Derive the reduction formula for $\int \sin^n x dx$.
10. Find the Fourier series for the function $x + x^2$ in $(-\pi, \pi)$.
Deduce that $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots = \frac{\pi^2}{12}$.
11. Solve $(D^2 + 3D + 2)y = e^{-2x} + \sin x$.
12. Solve the equation $(x^2 - y^2 - z^2)p + 2xyq = 2zx$.
13. (i) Show that $L(\cos at - \frac{1}{2} at \sin at) = \frac{s^3}{(s^2 + a^2)^2}$.
(ii) Evaluate $L(e^t \cos^3 t)$.
